Chapter 8

# Submesoscale processes and Mixing

J. Gula<sup>1</sup>,<sup>2</sup> J. Taylor<sup>3</sup>, A. Shcherbina<sup>4</sup>, & A. Mahadevan<sup>5</sup>

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<sup>1.</sup> Univ Brest, CNRS, IRD, Ifremer, Laboratoire d'Océanographie Physique et Spatiale (LOPS), IUEM, Brest, France

<sup>2.</sup> Institut Universitaire de France (IUF)

<sup>3.</sup> Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge CB3 0WA, UK

<sup>4.</sup> Applied Physics Laboratory, University of Washington, Seattle, Washington

<sup>5.</sup> Woods Hole Oceanographic Institution, Woods Hole, Massachusetts

#### ABSTRACT

In this chapter, we discuss the links between oceanic submesoscale (100 m–10 km) processes and mixing. Submesoscale currents occur on lateral scales of 100 m–10 km in the ocean and are associated with density fronts and filaments, vortices and topographic wakes at the surface and in the ocean's interior. In most cases, submesoscale processes do not directly contribute to mixing, however they have an important role in cascading energy and tracer variance from the largely adiabatic mesoscale down to the scales at which diapycnal mixing can occur. Submesoscale currents re-distribute water properties, including buoyancy, momentum, heat, freshwater, and biogeochemical tracers. While submesoscale instabilities enhance vertical exchange, they drive an efficient restratification of the upper ocean. They can also have a strong impact in the bottom boundary layer where they generate turbulent mixing and export mixed waters out of the bottom boundary layer.

We first present an overview of submesoscale dynamics, starting with frontogenesis and several important instability mechanisms that generate submesoscale currents in the ocean: mixed-layer baroclinic, gravitational, symmetric and inertial/centrifugal instabilities. Particular attention is paid to the complex role of turbulent mixing in the formation, evolution and decay of submesoscale features. We then discuss the impact of the different types of submesoscale processes on the redistribution of density and passive tracers, including impacts for some biogeochemical tracers and buoyant material.

#### **KEYWORDS**

Submesoscale currents, Frontogenesis, Mixed-layer instability, Symmetric instability, Centrifugal/Inertial instability, Restratification, Tracer dispersion, Vertical fluxes

## 8.1 INTRODUCTION

Submesoscale currents in the ocean take form of intense jets and vortices with horizontal scales of 100 m - 10 km and time scales of hours to weeks (Thomas et al., 2008; McWilliams, 2016). Almost invariably they are associated with the

<sup>5</sup> corresponding hydrographic features – fronts, filaments, and spirals of matching scales. This association is so tight that dynamic and hydrographic terms are commonly used interchangeably in the literature (e.g., "jets" and "fronts"). High resolution satellite observations of Sea Surface Temperature (SST) and ocean color or high resolution numerical models (Fig. 8.1) are exposing the ubiquity
 <sup>10</sup> of such submesoscale frontal features at the surface.

The upper end of the submesoscale is historically defined by the scales of the mesoscale eddies, which vary as the local Rossby deformation radius  $R_d$ , from roughly 10 km at high-latitudes to 200 km near to the equator (Chelton et al., 1998; LaCasce and Groeskamp, 2020). The lower end of the submesoscale

is typically taken as the scales corresponding to the turbulent boundary layer depth  $h_{bl} = 10 \text{ m} - 100 \text{ m}$ , below which the flow becomes more isotropic. Thus,

submesoscale currents occupy intermediate space and time scales between quasigeostrophic mesoscale eddies and the fully three-dimensional turbulence.

- Dynamically, submesoscale processes are characterized by order one Rossby and Froude numbers (Thomas et al., 2008). The Rossby number, arising from the relative scaling of the inertial and Coriolis terms in the equations of motion, is defined as Ro = U/fL, where U is the characteristic horizontal velocity scale, f is the local Coriolis frequency and L is the characteristic horizontal length scale. The Froude number, characterizing the balance of inertia and
- stratification effects, is defined as Fr = U/NH, where  $N = \sqrt{\partial b}/\partial z$  is the buoyancy frequency,  $b = -g\rho/\rho_0$  is the buoyancy,  $\rho$  is the density,  $\rho_0$  is a constant reference density, and *H* is the characteristic vertical scale. The order one Rossby and Froude numbers imply that stratification, rotation, and inertia are all important to submesoscale dynamics.
- The important role played by submesoscale currents has been realized over the last decade (McWilliams, 2016). Submesoscales can transfer energy from larger quasi-balanced motions to small-scale three-dimensional turbulence, thereby providing a route to dissipation (Müller et al., 2005). Submesoscale currents re-distribute water properties, including momentum, buoyancy, heat, freshwater,
- and biogeochemical tracers (Poje et al., 2014; Shcherbina et al., 2015; Mahadevan, 2016). The strong heterogeneities they generate at the ocean surface have important implications for modulating air-sea fluxes of energy and in structuring marine ecosystems (Lévy et al., 2018) and bacterioplankton communities (Fadeev et al., 2020). The strong vertical velocities they generate drive signif-
- <sup>40</sup> icant irreversible vertical fluxes of mass, buoyancy, and materials that control stratification of the upper ocean as well as exchanges between the surface layer and the ocean interior (Balwada et al., 2018; Su et al., 2018; Uchida et al., 2019; Mahadevan et al., 2020; Bachman and Klocker, 2020).
- Submesoscale currents are generated and influenced by a number of different processes, which are summarized in Fig. 8.2 and will be discussed in detail in the following section. The stirring induced by mesoscale eddies can generate density fronts and filaments (Hoskins and Bretherton, 1972; McWilliams, 1984). This can be described using quasi-geostrophic theories where it corresponds to a direct cascade of tracer variance toward smaller scales (see review in
- Lapeyre (2017) and Chapter 9 for a more detailed description). The fronts and filaments can then further intensify due to self-sustained frontogenesis (Hoskins and Bretherton, 1972). Ageostrophic effects are more important to 'submesoscale frontogenesis' when submesoscale currents deform fronts (Shakespeare and Taylor, 2013; Barkan et al., 2019).
- Another efficient mechanism to generate submesoscale currents is mixedlayer baroclinic instability (MLI) (Haine and Marshall, 1999; Boccaletti et al., 2007; Fox-Kemper et al., 2008). MLI is an extension of the classical geostrophic baroclinic instability, but with a smaller horizontal scale due to the reduced Rossby deformation radius in the mixed layer. However, since the corresponding
- Rossby number is typically O(1), ageostrophic effects are more pronounced in



**FIGURE 8.1** (a) Vertical vorticity  $\zeta$  normalized by f at the surface in the wintertime Gulf Stream in a submesoscale-resolving ( $\delta = 500$  m) simulation. (b) Vertical section of vertical vorticity along the dashed line in panel (a), and (c) Vertical section of vertical velocity.

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**FIGURE 8.2** Idealized depiction of various submesoscale processes discussed in this chapter. Convergent mesoscale strain drives frontogenesis. Surface cooling or a down-front wind can make the front unstable to symmetric instability (SI). The frontogenetic strain and vertical mixing drive an ageostrophic secondary circulation (ASC), which, in the latter case, can be described as a turbulent thermal wind (TTW) balance. Submesoscale eddies develop through mixed layer instability (MLI) which drives further frontogenesis and localizes boundary layer turbulence and subduction of water into the thermocline.

MLI compared to the mesoscale baroclinic instability. Submesoscale currents can also be generated by inherently ageostrophic "symmetric" instabilities triggered by atmospheric forcing at fronts (Taylor and Ferrari, 2009; Thomas and Taylor, 2010; D'Asaro et al., 2011). The ageostrophic nature of submesocale dy-

namics explains a number of profound characteristics of submesoscale features including intense upwelling/downwelling, rapid re-stratification, and production of small-scale turbulence.

In most cases submesoscale currents do not directly contribute to mixing in the form of tracer homogenization, which occurs near sub-millimeter Batchelor scales due to molecular diffusion. However, submesoscale dynamics have an important role in cascading energy and tracer variance from the largely adiabatic mesoscale down to scales where three-dimensional turbulence can take over

- (McWilliams et al., 2001). Submesoscale instabilities can facilitate a dynamical route to molecular diffusion by extracting energy from the geostrophically balanced flow and triggering secondary turbulent flows leading to small-scale turbulent mixing (Molemaker et al., 2010; D'Asaro et al., 2011; Brüggemann
- and Eden, 2015). Furthermore, submesoscale processes are typically associated with enhanced vertical velocities (Mahadevan and Tandon, 2006; Klein and Lapeyre, 2009) and vertical fluxes of heat, buoyancy and tracers in the mixed
- <sup>80</sup> layer (Mahadevan et al., 2012; Su et al., 2018). They can thus induce complex profiles of vertical stratification that influence vertical mixing in the surface layer and maintain elevated mixing efficiency at submesoscale fronts.

Submesoscale processes play a particularly important role in modulating the upper ocean stratification. Even though stratification changes are primarily

- driven by air-sea exchanges and vertical mixing, lateral stirring becomes increasingly important near density fronts (Rudnick and Ferrari, 1999; Ferrari and Rudnick, 2000). Submesoscale processes alter the horizontal and vertical density gradients in a number of interrelated and competing ways: Frontogenesis sharpens horizontal gradients of density and may also alter the vertical strati-
- fication if frontogenetic strain is depth-dependent. At the same time, submesoscale ageostrophic secondary circulation associated with frontogenesis, MLI and symmetric instability (SI) tends to decrease isopycnal slope in the upper ocean, partially transforming horizontal density gradients into vertical – a process commonly described as submesoscale frontal slumping and restratification.
- <sup>95</sup> Submesoscale dynamics have been originally studied in the open ocean surface boundary layer, although they are also prevalent in coastal or estuarine environments. The local Rossby deformation radius on the continental shelf can be on the order of 1-10 km or smaller, such that structures at this scale may be classified as mesoscale in the literature. However, the Rossby and Froude
- numbers nearshore can reach and exceed O(1) values typical of open ocean submesoscale regimes (*e.g.*, Capet et al., 2008a; Dauhajre et al., 2017; Wang et al., 2021). Thus, littoral dynamics share many processes with open ocean submesoscale dynamics, albeit modified by the strong influence of topographic, wave-driven, tidal, and freshwater runoff effects.

- <sup>105</sup> Energetic submesoscale currents can also be found at the bottom of the deep ocean in the presence of steep topography as on continental slopes, seamounts and ridges. An illustration showing submesoscale currents in a numerical model at 1500 m depth around the Mid-atlantic ridge is shown in Fig. 8.3. High resolution numerical models have highlighted efficient mechanisms for topographic
- generation of submesoscale currents through interactions of geostrophic flows with steep topographic slopes (Molemaker et al., 2015; Gula et al., 2015b), ridges (Vic et al., 2018), and seamounts (Srinivasan et al., 2019). These interactions can lead to elevated local kinetic energy dissipation (Gula et al., 2016) and diapycnal mixing (Dewar et al., 2015) through triggering of centrifugal instability or in-
- tense horizontal shear instability and to the formation of submesoscale coherent vortices. Observations have recently confirmed that bottom currents interacting with sloping topography can trigger submesoscale instabilities with important implications for mixing and upwelling of deep-ocean waters (Ruan et al., 2017; Naveira Garabato et al., 2019). Theoretical and process studies are beginning
- to highlight the full extent of the role played by submesoscale processes in the bottom boundary layer (Wenegrat et al., 2018a; Wenegrat and Thomas, 2020). Furthermore, submesoscale baroclinic instability of the bottom boundary layer might be instrumental in driving restratification in the deep ocean and exporting mixed water from the bottom boundary layer (Callies, 2018; Wenegrat et al., 2018).
- 125 2018a). These results are particularly timely because of the recent realization that the energetic mixing near ocean boundaries plays a fundamental role in driving the global ocean circulation, as detailed in Chapters 3 and 7 of this book. The role played by bottom submesoscale processes in this picture is still largely unknown.
- Field observations of submesoscale phenomena are complicated by their small horizontal scales, rapid evolution, and spatial heterogeneity. Much of our understanding of submesoscale dynamics has been obtained from numerical modelling (Fig. 8.1), either through dedicated process studies (*e.g.*, Boccaletti et al., 2007) or realistic high-resolution simulations (*e.g.*, Capet et al., 2008b).
- <sup>135</sup> Observational verification of this understanding, however, remains a challenge. While satellite SST or ocean color routinely reveal an abundance of submesoscale structures at the surface, they cannot be used to reconstruct the underlying velocity fields. Furthermore, the footprints of the current generation of satellite altimeters ( $\approx 100$  km) is unable to resolve submesoscale currents. Satellite mea-
- <sup>140</sup> surements from the Surface Water and Ocean Topography mission (SWOT, Fu and Ferrari, 2008) will soon provide a global coverage of Sea Surface Height (SSH) at better resolution (15-30 km, Morrow et al. 2019). However, reconstructing the surface velocity from SSH at these scales remains a challenging task due to the presence of internal waves and other unbalanced motions with
- similar spatial scales (Torres et al., 2018). Promising results have been obtained for the observation of intense submesoscale fronts with airborne optical and radar measurements of their surface roughness signature (Rascle et al., 2017, 2020), but they are limited to a small number of examples so far.



**FIGURE 8.3** Instantaneous relative vorticity  $\zeta = v_x - u_y$  at 1500 m depth over the Mid-Atlantic Ridge. Data from a numerical simulation with  $\delta x = 750$  m horizontal resolution. Image adapted from Vic et al. (2018).

Only a few dedicated observational programs have been able to acquire data with enough spatial and temporal resolution to allow a quantitative characterisation of submesoscale currents in the surface layer, *e.g.*, AESOP (D'Asaro et al., 2011; Johnson et al., 2020a), LATMIX (Shcherbina et al., 2013), OSMOSIS (Buckingham et al., 2016), ASIRI (Wijesekera et al., 2016), CARTHE-LASER (D'Asaro et al., 2020), and CALYPSO (Mahadevan et al., 2020). Such programs

- <sup>155</sup> usually require a combination of mooring arrays, multiple ships, autonomous underwater vehicles, or swarms of surface drifters to allow for a computation of submesoscale gradients of velocity and tracers. Observations of submesoscale currents at the bottom of the ocean are even more difficult to obtain and the examples are still rare (Naveira Garabato et al., 2019).
- In the following section, we review the important mechanisms driving the formation, evolution, and decay of submesoscale fronts. These include frontogenesis in section 8.2.1 and the instabilities that develop on submesoscale fronts in section 8.2.2. Aspects specific to the bottom boundary are developed in section 8.2.3. The evolution of fronts in the presence of turbulent mixing is discussed in
- section 8.2.4, and finally the decay of submesoscale fronts is discussed in section 8.2.5. In section 8.3, we discuss the impact of the different types of submesoscale processes on the redistribution of density, focusing in particular on the effects on the restratification of the surface layer, but also on the mixing and restratification induced by submesoscale processes in the bottom boundary layer. In section 8.4,
- the impact on the redistribution of passive tracers is discussed, including impacts for some biogeochemical tracers and buoyant material. Finally we present our conclusions and perspectives in section 8.5.

# 8.2 LIFE-CYCLE OF SUBMESOSCALE FRONTS

#### 8.2.1 Frontogenesis

- Open ocean fronts develop and intensify through a process known as frontogenesis. The mathematical theory of frontogenesis, which describes the intensification of cross-front density gradients in response to an imposed background flow, was originally developed in the atmospheric context (Hoskins and Bretherton, 1972; Hoskins, 1982) and later applied to the upper ocean (Macvean and Woods,
- <sup>180</sup> 1980; Lapeyre and Klein, 2006; Capet et al., 2008c). An extensive review of oceanic frontogenesis has recently been published by McWilliams (2021), we briefly recall the important aspects of frontogenesis below.

A classical description of frontogenesis involves the sharpening of favorably aligned lateral density gradients by a straining flow, disruption of geostrophic balance for the along-front flow, and generation of an ageostrophic secondary circulation (ASC), see Fig. 8.2. This secondary circulation acts to restore geostrophic balance by advectively restratifying the flow, *i.e.*, tilting the isopycnals toward the horizontal by bringing warm/light water over the top of cold/dense water. The ASC thus forms an overturning cell in the cross-front/vertical plane,

- with upwelling (w' > 0) on the light side  $(\rho' < 0 \text{ or } b' > 0)$  and downwelling (w' < 0) on the dense side  $(\rho' > 0 \text{ or } b' < 0)$ , where *w* is the vertical velocity and primes denote deviations from a cross front average. The associated vertical buoyancy flux is thus always positive, i.e. w'b' > 0, corresponding to restratification of the front.
- <sup>195</sup> A canonical setup to study frontogenesis considers a density front embedded in a large-scale horizontal flow with a uniform strain rate:  $u_d = -\alpha x$ ,  $v_d = \alpha y$ , as illustrated in Fig. 8.4a. This configuration is well suited for mesoscale strain-induced frontogenesis, which is one of the fundamental factors leading to submesoscale currents. For a quasi-geostrophic flow, strain-induced frontogenesis causes the cross-front gradient to increase at an exponential rate (*e.g.*,

 $\partial_x C \sim \exp \alpha t$  for a tracer *C*) (Washington, 1964).

On the dense side of a finite-width front, the ASC is convergent at the ocean surface (see Fig. 8.4). This amplifies the convergence associated with the large-scale strain flow and accelerates frontogenesis. Using the inviscid semigeostrophic equations, Hoskins and Bretherton (1972) showed that this leads to super-exponential intensification of the density gradient and the collapse of the front into a singularity in finite time. A similar result was found in the generalized theory of Shakespeare and Taylor (2013) which included gravity waves and other ageostrophic effects. The asymptotic model derived by Barkan et al. (2019) even

- shows that when  $Ro \sim 1$  the sharpening rate is primarily determined by the nearsurface convergent motions associated with the ASC, rather than the large-scale strain flow. A bulk estimate for the vertical buoyancy fluxes of a front undergoing submesoscale frontogenesis is shown to be:  $w'b' \sim -Hl(t)\delta(t)\partial_x b(t)$ , with  $\delta(t) < 0$  the velocity divergence due to the ASC,  $l(t) \approx l(t_0)(1 + \delta(t_0)t)$  the
- width of the front at a time  $t > t_0$ . Therefore, any pre-existing density front, for example generated by the stirring of mesoscale eddies, may rapidly form an intense submesoscale front with order one *Ro* and further sharpen at a super-exponential rate.

A variant of frontogenesis applicable to dense filaments – sometimes called filamentogenesis – has been proposed by McWilliams et al. (2009). A dense filament corresponds to a surface density maximum formed by two parallel fronts with opposite-sign density gradient, as shown in Fig. 8.4b. The deformation flow acting on a favorably aligned dense filament causes an even more rapid narrowing and stronger surface convergence and downwelling at its center than for an isolated front of similar scale and *Ro*. Instantaneous values of the vertical velocity at the center of dense filaments can reach  $\sim 1 \text{ cm s}^{-1}$  in realistic submesoscale-resolving simulations (Gula et al., 2014).

In general, any ASC in a finite-width front will necessarily have a zone of surface convergence, and therefore may contribute additional frontogenetic feedback. An example of this will be discussed in section 8.2.4 dealing with the ASC

induced by vertical mixing.

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**FIGURE 8.4** Sketches of surface-layer frontogenesis caused by a large-scale deformation flow for (a) a front and (b) a dense filament, adapted from McWilliams (2016).

# 8.2.2 Instability of surface boundary layer fronts

Once fronts form and intensify through the process of frontogenesis, they can become susceptible to a variety of instabilities which generate additional submesoscale currents. These instabilities include: mixed-layer instability (MLI); symmetric instability (SI); ageostrophic anticyclonic instability (McWilliams et al., 2004); and horizontal shear instability (Munk et al., 2000).

<sup>240</sup> In this section, we briefly describe the theory for the two most studied submesoscale instabilities: MLI and SI. Although the focus in this section will largely be on processes in the upper ocean, similar physical mechanisms are also active in the bottom boundary layer, as will be discussed in section 8.2.3.

## 8.2.2.1 Mixed-layer baroclinic instability

- Mixed-layer instability (MLI) is an upper-ocean equivalent of the classical interior baroclinic instability (Haine and Marshall, 1999), as illustrated in Fig. 8.5. It is one of the most important sources of submesoscale currents in the surface mixed-layer, and it has been extensively studied over the last decade using theory, idealised numerical simulations (Boccaletti et al., 2007; Fox-Kemper et al., 2008; Calliag et al., 2016), and realistic submesoscale accelulation pumpriced.
- et al., 2008; Callies et al., 2016), and realistic submesoscale resolving numerical simulations (Capet et al., 2008c).

Baroclinic instabilities in the ocean interior are the primary source for the generation of mesoscale eddies at horizontal scales around or larger than the Rossby deformation radius:

$$R_{int} = \frac{N_{int}H_{tot}}{f},\tag{8.1}$$

where  $N_{int}$  is the stratification in the ocean interior and  $H_{tot}$  the ocean depth. MLI is a similar mechanism taking place in the weakly stratified surface layer,



**FIGURE 8.5** (a) Time sequence of the surface density anomaly showing the evolution of MLI in an idealized simulation of a front. (b) Evolution of the across front density and (c) of the vertical stratification. Adapted from Mahadevan et al. (2010).

which has its own deformation radius,

$$R = \frac{NH}{f} \tag{8.2}$$

where *N* and *H* are now the stratification and thickness of the weakly stratified surface layer. *R* is typically much smaller than  $R_{int}$  because of the relative smallness of the mixed layer stratification *N* and thickness *H*. Typical values of  $N = 10^{-3} \text{ s}^{-1}$ , H = 100 m and  $f = 10^{-4} \text{ s}^{-1}$  lead to R = 1 km, which is well within the submesoscale range.

Submesoscale MLI can be analyzed to leading order using the Eady model (Eady, 1949). Although the ageostrophic secondary circulation can be large during submesoscale frontogenesis (Barkan et al., 2019), most theoretical studies of submesoscale instability have considered a balanced basic state. The basic state in the Eady model consists of a fluid with constant horizontal and vertical buoyancy gradients bounded from above and below by flat, rigid surfaces. The basic state velocity has a constant vertical shear in thermal wind balance with the horizontal buoyancy gradient. Specifically, if the basic state buoyancy is

$$b = N^2 z - M^2 y, (8.3)$$

then the basic state geostrophic velocity is

$$u = \frac{M^2}{f}z,\tag{8.4}$$

where in this case z can be defined with respect to an arbitrary reference level of no motion.

As discussed in Eady (1949) and Stone (1966), there is one non-dimensional parameter in the system describing the evolution of linear, inviscid perturbations to this basic state. This parameter can be formulated as a 'balanced Richardson number',

$$Ri \equiv \frac{N^2}{u_7^2} = \frac{N^2 f^2}{M^4},$$
(8.5)

where  $u_z$  is the thermal wind shear. Note that Ri is equivalent to the gradient Richardson number formed with the thermal wind shear. If we use the thermal wind to define a characteristic velocity scale,  $U = M^2 H/f$ , where H is the vertical distance between the top and bottom boundaries, and set a characteristic horizontal length scale based on the isopycnal slope, i.e.  $L = N^2 H/M^2$ , then we can relate the Rossby number to the balanced Richardson number,

$$Ro \equiv \frac{U}{fL} = \frac{M^4}{f^2 N^2} = \frac{1}{Ri}.$$
 (8.6)

The analysis in Eady (1949) assumed that  $Ri \gg 1$  and hence  $Ro \ll 1$ , while Stone (1966) generalized this to arbitrary Ri and Ro. When  $Ri \gg 1$ , the most unstable mode in the Eady model is independent of the cross-front direction (the *y*-direction in the basic state given above) and corresponds to the classical baroclinic instability. In this context, MLI can be viewed as baroclinic instability in the limit when  $Ri, Ro \sim 1$ , both characteristic of submesoscales in the mixed layer.

The wavelength of the most unstable perturbation for baroclinic instability is  $L \approx 4R$ , assuming that  $Ri \gg 1$  as in Eady (1949). Taking into account ageostrophic effects, the wavelength of the fastest-growing MLI mode becomes  $L_{MLI} \approx 4\sqrt{1 + Ri^{-1}R}$  (Stone, 1966; Nakamura, 1988), such that the instability is shifted to larger scales at small Ri if R is fixed. This scaling, with a typical value Ri = 0.8, has been used to estimate the surface MLI wavelength on a global scale by Dong et al. (2020b). The mixed-layer depth and stratification have been computed either directly from Argo profiles or from 1D simulations of the Generalized Ocean Turbulence Model (GOTM) embedded in the outputs of

- <sup>300</sup> a global MITgcm simulation at submesoscale-permitting resolution (LLC4320, see Su et al. (2018)), as shown in Fig. 3 and 4 of Chapter 4. The results obtained for  $L_{MLI}$  with GOTM and a KPP parameterization for vertical mixing are reproduced in Fig. 8.6a. The zonal median MLI wavelength varies from about 30 km in the tropics to 1 km at high-latitudes. Given that the grid-spacing
- of a model needs to be at least  $L_{MLI}/8$  to properly resolve the eddies generated due to MLI, the requirements are still pretty high for models to be able to resolve MLI on a global scale.

MLI draws its energy from the available potential energy associated with horizontal buoyancy gradients – and converts it to kinetic energy. The energy

<sup>310</sup> source term in the equation of evolution for the perturbation kinetic energy is the buoyancy flux, w'b', where perturbations to the background flow are denoted  $(\cdot)'$  (Capet et al., 2008c). The buoyancy flux associated with MLI is thus always positive and restratifies the mixed layer by distorting and tilting isopycnal surfaces (Fig. 8.5). Re-stratification by MLI represents a leading-order process in the mixed-layer buoyancy budget, as discussed in Sec. 8.3.

The conversion of available potential energy to kinetic energy happens near the instability scale. From there we may expect two possible non-linear energy cascades: an inverse energy cascade towards larger scales – typical of geostrophic turbulence (see review in Klein et al., 2019) –, and a forward energy cascade

- driven by ageostrophic motions and loss of balance (Capet et al., 2008d). MLI transfers energy preferentially to larger scales (Boccaletti et al., 2007; Fox-Kemper et al., 2008), as visible in Fig. 8.5. Interactions between submesoscale eddies generated by MLI lead to an inverse cascade of energy, from the scale corresponding to the local wavelength of the fastest growing mode of MLI towards the mesoscale. This process helps to energize mesoscale eddies (Qiu
- et al., 2014; Sasaki et al., 2014; Schubert et al., 2020) and may explain the interannual to decadal variations of the mesoscale kinetic energy (Sasaki et al., 2020). However, the submesoscale eddy field generated as a result of MLI also develops sharp frontal features with active frontogenesis, which can lead to secondary instabilities and small-scale turbulence, and feed the forward cascade of energy (Schubert et al., 2020), as discussed in Sec. 8.2.5.

The available potential energy density at a front scales as  $H^2 |\nabla_h b|$ . The depth of the mixed-layer is thus a critical parameter controlling the energy of submesoscale eddies generated by MLI. This explains why submesoscale flows are expected to be stronger in winter, when the mixed-layer deepens due to the strong negative buoyancy forcing, than in summer. This seasonality is confirmed by both the numerical simulations (Mensa et al., 2013; Sasaki et al., 2014; Brannigan et al., 2015; Ajayi et al., 2021) and in-situ observations (Callies et al., 2015). In winter, the energized submesoscale flows produce surface kinetic energy spectra that scale like  $k^{-2}$  at scales below 100 km, with *k* the horizontal wavenumber, which is typical of active submesoscale regimes. In summer, the spectra are steeper and scale like  $k^{-3}$ , which is typical of interior quasigeostrophic turbulence. More precisely, a global analysis using outputs from the submesoscale-permitting LLC4320 simulation has highlighted two phases

- in this seasonal transition (Khatri et al., 2020). In late autumn the spectra first flatten as  $k^{-2}$  at scales < 50 km, but still follow a  $k^{-3}$  slope at larger scales (100-300 km). In late winter, the spectra flattens as  $k^{-2}$  also at large scales due to the inverse energy cascade initiated by MLI energizing the mesoscales. There is also a time-lag – about one month in the Kuroshio region – between the
- mixed-layer thickness maximum and the submesoscale energy peak due to the competition between the production of eddy kinetic energy due to the vertical buoyancy fluxes and the nonlinear energy cascade to larger scales (Dong et al., 2020a). The surface MLI wavelength, which scales linearly with H, also has

a strong seasonality with a median value 1.6 times smaller in summer (10 km) than winter (16 km) globally (Fig. 8.6a).

Submesoscale baroclinic instability modes can sometimes extend below the mixed-layer for particular stratification profiles. This can happen in the presence of a weakly-stratified transition layer between the mixed layer and the thermocline, as observed by Zhang et al. (2020). The presence of a weakly-stratified

<sup>360</sup> sublayer and an equatorward buoyancy gradient can also lead to the onset of Charney baroclinic instability, leading to an intensification of near-surface frontal activity (Capet et al., 2016).

## 8.2.2.2 Symmetric Instability

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When ageostrophic perturbations are considered in the linear stability analysis of the Eady model described previously, an additional set of instabilities are permitted. This was shown by Stone (1966, 1970, 1972) in a series of papers on non-geostrophic instability in the Eady model.

When Ri < 1, an ageostrophic instability develops where the most unstable perturbations are independent of *x* (the cross-front direction)<sup>6</sup> Stone (1966) and

Hoskins (1974) refer to this mode as 'symmetric instability' - a term that originated in studies of growing axisymmetric perturbations to a circular baroclinic vortex (Eliassen and Kleinschmidt, 1957; Ooyama, 1966).

In an unbounded, inviscid fluid, the most unstable mode of symmetric instability (hereafter SI) has motion that is aligned with isopycnals (Stone, 1966;

- Taylor and Ferrari, 2009). As a result, the buoyancy perturbations associated with SI modes are typically small. Whereas the baroclinic instabilities (including MLI) gain energy predominately from background potential energy, SI modes gain energy primarily at the expense of the thermal wind shear (Taylor and Ferrari, 2010).
- Hoskins (1974) showed that the criterion for SI can be written fq < 0 where  $q = (\omega + f\hat{\mathbf{k}}) \cdot \nabla b$  is the Ertel potential vorticity (PV) and f is the Coriolis parameter<sup>7</sup>. This immediately presents a paradox: Since PV is materially conserved in an adiabatic, inviscid fluid, no re-arrangement of fluid parcels within a region with fq < 0 will change the bulk PV (Thorpe and Rotunno, 1989).

<sup>385</sup> A resolution of this paradox was proposed by Taylor and Ferrari (2009) who showed that the along-isopycnal motions associated with SI become unstable to a secondary Kelvin-Helmholtz shear instability. The resulting small-scale turbulence quickly increases fq by exchanging PV with a neighboring stable region (*e.g.*, the pycnocline) or driving a stabilising PV flux through the ocean surface.

<sup>6.</sup> Note that Stone (1966) also refers to Kelvin-Helmholtz instabilities, but Vanneste (1993) showed that these do not develop in the Eady model.

<sup>7.</sup> Note that a more general criterion for SI can be introduced for curved fronts in cyclogeostrophic or gradient wind balance. The resulting expression becomes (1 + Cu) f q < 0, where Cu is a nondimensional number quantifying the curvature of the flow, as discussed in Buckingham et al. (2021a,b)



**FIGURE 8.6** Global distributions of the fastest-growing wavelength (in km) for (a,b) MLI, (c,d) BMLI, and (e-f) SI, and relative likelihood (%) of SI (g-h). Results in (left) winter (February in the Northern Hemisphere and August in the Southern Hemisphere) and (right) summer (August in the Northern Hemisphere and February in the Southern Hemisphere). Figure adapted from Dong et al. (2020b) and Dong et al. (2021).

SI can also be viewed as a hybrid of inertial and gravitational instability (Haine and Marshall, 1999). Due to the close connection with gravitional instability, SI is sometimes refered to as 'slantwise convection' (e.g. Straub and Kiladis, 2002; van Haren and Millot, 2009), although as discussed below it is important to note that the energetics of SI are distinct from convection. Inertial instability arises when the vertical component of the relative vorticity is anticyclonic and larger in magnitude than the Coriolis parameter, i.e.  $\zeta/f < -1$ . When the stratification is unstable ( $N^2 < 0$ ) gravitational (or Rayleigh-Taylor)

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instability can develop. For inviscid motions that are independent of x, the absolute momentum,  $\mathcal{M} \equiv u - f y$ , is conserved,

$$\frac{D\mathcal{M}}{Dt} = 0, \tag{8.7}$$

where D/Dt is the material derivative. In this case, the Ertel PV can be written

$$q = \mathcal{M}_{y}b_{z} - \mathcal{M}_{z}b_{y}. \tag{8.8}$$

For simplicity, consider the Northern Hemisphere (f > 0) where SI develops when q < 0 or

$$\frac{\mathcal{M}_y}{\mathcal{M}_z} < \frac{b_y}{b_z}.$$
(8.9)

<sup>405</sup> In other words, SI can occur when isopycnals are steeper than surfaces of constant absolute momentum.

Given the close relationship between gravitational, inertial, and symmetric instability, a natural question is how to identify the dominant instability from a given set of conditions (*e.g.*, in observations or an ocean model). This is

<sup>410</sup> particularly relevant within strong fronts where all three instabilities can result in slantwise motion. The potential vorticity is not sufficient to distinguish between these instabilities since gravitational and inertial instability are also typically associated with fq < 0 (with  $fN^2 < 0$  in the case of gravitational instability and  $f\zeta < 0$  in the case of inertial instability). One approach, which was utilized <sup>415</sup> by Thomas et al. (2013) is to classify the dominant instability associated with a

given basic state using the energetics of the most unstable mode.

In a barotropic fluid, gravitational instability converts background potential energy into kinetic energy through the vertical buoyancy flux (w'b' > 0), while inertial instability grows via lateral shear production. As noted above, SI predominately extracts energy from the vertical shear associated with the thermal wind via geostrophic shear production (Taylor and Ferrari, 2010). By identifying the energy source associated with the most unstable perturbations, the dominant instability can be identified from a given basic state.

As was shown by Thomas et al. (2013), for a basic state that is in thermal wind balance, the dominant type of instability depends on the balanced Richardson number (5). Thomas et al. (2013) introduced what we call the 'Thomas angle', Th, where

$$\mathrm{Th} \equiv \tan^{-1} \left( -\frac{|\nabla_h b|^2}{f^2 N^2} \right). \tag{8.10}$$

The Thomas angle is analogous to the Turner angle (often denoted Tu) which is used to distinguish different types of double-diffusive instabilities.

The Thomas angle re-maps the possible values of  $Ri \in (-\infty, \infty)$  to  $-\pi \leq$ Th  $\leq 0$ . For a basic state consisting of uniform gradients in velocity and buoyancy, the flow is unstable when Th < Th<sub>c</sub>, where

$$Th_c \equiv \tan^{-1}\left(-\frac{\zeta}{f}\right),\tag{8.11}$$

is the critical angle. Figure 8.7 shows regions of gravitational instability (GI), symmetric instability (SI), and inertial instability (II). When the basic state vertical vorticity is anticyclonic, inertial/symmetric instability (II/SI) occurs when  $-45^{\circ} < \text{Th} < \text{Th}_c$ . In this region the lateral shear production (*LSP*) is the dominant energy source for the growing perturbations, although the geostrophic shear production (*GSP*) also contributes. For a stably stratified barotropic fluid ( $N^2 > 0$  and  $|\nabla b| = 0$ ), the Thomas angle is Th = 0, and instability is only perceptible if The  $\geq 0$ , which corresponds to  $\zeta < -f$  the usual aritation for

<sup>440</sup> possible if Th<sub>c</sub> > 0, which corresponds to  $\zeta < -f$ , the usual criterion for inertial instability.

Although an unstable buoyancy profile ( $N^2 < 0$ ) corresponds to Th  $< -\pi/2$ , the buoyancy flux (BFLUX) is the dominant source of energy only for Th  $< -3\pi/4$ . When  $-3\pi/4 <$  Th  $< -\pi/4$  for anticyclonic vorticity and  $-3\pi/4 <$ 

- <sup>445</sup> Th < Th<sub>c</sub> for cyclonic vorticity, the GSP is the dominant source of perturbation kinetic energy. Within these limits, Thomas et al. (2013) distinguish between SI/GI when  $N^2 < 0$  and SI when  $N^2 > 0$ . Although the linear stability analysis was performed for a simple basic state with uniform velocity and buoyancy gradients, Thomas et al. (2013) showed that the Thomas angle was able to identify
- 450 various dynamical regimes when applied *pointwise* to large-eddy simulations of the Gulf Stream front.

#### 8.2.2.3 Forced symmetric instability

Since the criterion for SI depends on the sign of the potential vorticity, and since PV is materially conserved, the development of SI is closely tied to boundary forcing that is capable of changing the bulk PV. Further, since the growth rate of SI is relatively fast (with a characteristic timescale ~ 1/f), simulations and observations indicate that SI can quickly respond to de-stabilizing forcing and maintain  $fq \approx 0$  (*e.g.*, Thomas and Taylor, 2010; Thomas et al., 2013, 2016). Following Taylor and Ferrari (2010), we use 'forced symmetric instability' (or forced SI) to refer to the nonlinear manifestation of symmetric instability that

develops in response to de-stabilizing surface forcing. Thomas (2005) discussed the conditions required for destruction of PV by

surface forcing and showed that fq is reduced when the surface of the ocean is

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**FIGURE 8.7** Regimes of gravitational instability (GI), symmetric instability (SI) and inertial instability (II) as a function of the Thomas angle (Th) when the vertical component of the relative vorticity ( $\zeta$ ) is anticyclonic (left) and cyclonic (right). In each region, the dominant source of energy is labeled as follows: Buoyancy flux (*BFLUX*), Geostrophic shear production (*GSP*), and lateral shear production (*LSP*). Adapted from Thomas et al. (2013).

cooled by losing heat to the atmosphere, or when the surface wind stress points
in the direction of the thermal wind - a so called 'downfront wind'. In the case of a downfront wind, dense water tends to be drawn over light water by the cross-front Ekman flow acting on the horizontal density gradient associated with the front. When sampled at a fixed position, this cross-front advection will result in a decrease in the surface buoyancy. The rate of change in buoyancy induced
by the cross-front Ekman flow can be quantified through the Ekman buoyancy

flux (EBF):

$$\text{EBF} \equiv \mathbf{M}_E \cdot \nabla_h b, \qquad (8.12)$$

where

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$$\mathbf{M}_E = \boldsymbol{\tau}_w \times \frac{f \hat{\mathbf{k}}}{\rho_0 f^2},\tag{8.13}$$

is the Ekman transport,  $\tau_w$  is the wind stress,  $\nabla_h b$  is the horizontal buoyancy gradient, f is the Coriolis parameter, and  $\hat{\mathbf{k}}$  is the vertical unit vector. For a boundary layer of thickness H, the rate of change of PV scales with the sum of the EBF and the surface buoyancy flux,  $B_0$ :

$$\frac{Dq}{Dt} \sim -\frac{f}{H^2} \left( \text{EBF} + B_0 \right). \tag{8.14}$$

Hence, when EBF +  $B_0 > 0$ , fq will be reduced and conditions could become favorable for SI. It is worth emphasizing that the EBF is an *advective* buoyancy flux and that advection does not change the integrated buoyancy. However, the appearance of the EBF in Eq. 8.14 shows that the EBF is generally associated with a change in the bulk PV. This is due to the fact that a downfront wind stress induces a frictional PV flux that removes PV from the ocean (Thomas, 2005).

As noted above, fq < 0 is a necessary but not sufficient condition for SI and the dominant instability will depend on the Thomas angle. For example, if  $\nabla_h b = 0$  surface cooling  $(B_0 > 0)$  will decrease fq, but the flow will become susceptible to gravitational instability (convection) rather than SI. Taylor and Ferrari (2010) used idealized simulations to study buoyancy and wind-driven convection within a frontal zone. They found that like convection, SI acts fast enough to keep the PV close to zero in a 'low PV layer'. PV conservation then allows a prediction for the deepening of the low PV layer, given the rate of PV destruction due to the surface forcing.

Taylor and Ferrari (2010) found that for surface cooling and downfront winds, the low PV layer can be further decomposed into two layers as shown in Figure 8.8. In a 'convective layer', near the surface, stratification is weak, the buoy-

ancy flux is positive, and convective plumes are visible. Note that despite its name, turbulence generated by wind and/or wave breaking can dominate in the 'convective layer', and any plumes might be strongly distorted by the associated shear. Below the convective layer, SI develops, resulting in a stable stratification. In this 'forced SI layer', small-scale turbulence is generated by secondary shear instabilities that develop between the SI cells. This small-scale turbulence acts in the sense to mix the stable stratification, and hence the buoyancy flux is negative. In the forced SI layer, a cross-front shear (which will be described later) maintains the stable stratification.

Taylor and Ferrari (2010) derived a scaling for the depth of the convective layer h:

$$\frac{|\nabla_h b|^2}{f^2} (B_0 + \text{EBF})^{1/3} h^{4/3} = c \left[ (B_0 + \text{EBF}) \left( 1 - \frac{h}{H} \right) \right],$$
(8.15)

where  $c \approx 14$  is an empirical scaling coefficient. For a known low PV layer depth, *H*, horizontal buoyancy gradient,  $|\nabla_h b|$ , and surface and Ekman buoyancy flux,  $B_0$  and EBF, Eq. 8.15 can be solved numerically to find *h*. This provides a means for identifying when SI will be active under a given set of conditions. At <sup>510</sup> a strong front and/or with weak surface forcing,  $h/H \rightarrow 0$ , and SI will develop throughout the low PV layer. However, when the horizontal buoyancy gradient is weak or forcing is sufficiently strong,  $h/H \rightarrow 1$ , and the low PV layer is expected to be weakly stratified.

Taylor and Ferrari (2010) used a turbulent Ekman balance (which is discussed below in Section 8.2.4) to show that the sum of the geostrophic shear production and buoyancy flux in a boundary layer with forced SI is a linear function of depth within the low PV layer, specifically

$$GSP + BFLUX \simeq (B_0 + EBF)\left(\frac{z+H}{H}\right).$$
 (8.16)

Thomas et al. (2013) proposed a model profile for the GSP by further assuming that the buoyancy flux takes the following linear profile within the convective



**FIGURE 8.8** Schematic showing the structure of forced symmetric instability as described by Taylor and Ferrari (2010). Solid curves show the buoyancy flux (BFLUX), geostrophic shear production (GSP), and their sum as calculated from the large-eddy simulation of the response of the Gulf Stream to a storm as reported in Thomas et al. (2016). Dashed lines show the SI parameterization further described in Bachman et al. (2017a). The surface buoyancy flux,  $B_0$ , the Ekman buoyancy flux, EBF, and their sum are also labeled.

layer:

$$BFLUX \simeq B_0 \frac{z+h}{h}.$$
(8.17)

These model profiles are shown in Figure 8.8 and compared with the LES in Thomas et al. (2013). Bachman et al. (2017a) used this as a basis for a parameterization for SI and implemented it in the MITgcm.

<sup>525</sup> Observational evidence for SI typically consists of finding of signs of enhanced ventilation, fine-scale interleaving and small-scale mixing within stratified baroclinic fronts. Early suggestions that SI (under the name of 'slantwise convection') may be partially responsible for ventilation of the Labrador Current was reported in Straneo et al. (2002). D'Asaro et al. (2011) and Thomas

- et al. (2013) observed regions with fq < 0 in the Kuroshio and Gulf Stream fronts, respectively. D'Asaro et al. (2011) and Thomas et al. (2016) observed elevated dissipation rates within these regions, providing indirect evidence for geostrophic shear production associated with SI.
- Several studies from the OSMOSIS project have shown evidence for SI in the subtropical northeast Atlantic. Using a full year of glider and mooring observations, Thompson et al. (2016); Buckingham et al. (2019); Yu et al. (2020) found a stratified low PV layer in the winter with scalings that were consistent with the model and theory in Taylor and Ferrari (2010). Yu et al. (2019b) found evidence for wind-forced SI at a transient front in the same region, as
- <sup>540</sup> illustrated in Fig. 8.9. In-situ observations from the mooring array were used to compute the vertical stratification, the lateral buoyancy gradient, and the most likely instability (GI,SI,II) according to the classification described in Fig. 8.7. The mixed layer was favorable to GI triggered by atmospheric cooling (~ 200 W m<sup>-2</sup>) between 3 and 7 April 2013, which resulted in a deepening of the mixed
- <sup>545</sup> layer down to almost 300 m. A strong lateral buoyancy gradient, generated by the confluence of mesoscale eddies, developed between 8 and 11 April 2013. Persistent down-front winds during this period led to the generation of SI (Fig. 8.9c) and an EBF ~ 650 W m<sup>-2</sup>. The SI event was also associated with elevated glider-derived turbulent dissipation rates. Other evidence of SI were found by
- Ramachandran et al. (2018) in a shallow front in the Bay of Bengal, by Peng et al. (2020) in a density filament in the Benguela upwelling system, by Koenig et al. (2020) in a thermohaline front caused by sea ice melt in the Nansen Basin, and by Bosse et al. (2021) around a deep convection area in the northwestern Mediterranean Sea. Together these studies suggest that SI does not require strong climatological fronts like the Gulf Stream and Kuroshio, and instead can occur

in typical open ocean conditions.

Perhaps the most direct evidence for SI comes from observations of its influence on temperature and tracer. Savelyev et al. (2018) observed step-like patterns in the surface temperature in the southern Gulf Stream from airborne

thermal imagery. These features closely resemble the feature seen in numerical simulations of SI (*e.g.*, Stamper and Taylor, 2017) and concurrent ship-based measurements confirmed that conditions were favorable for SI. Wenegrat et al.



**FIGURE 8.9** Time series of (a) vertical buoyancy stratification N<sup>2</sup>, (b) lateral buoyancy gradient  $|\nabla_h b|$ , and (c) submesoscale instability category at the OSMOSIS central mooring site from 3 to 12 April 2013. The white line indicates the mixed layer depth and the blue line indicates the convective layer depth. Isopycnals are overlaid as black contours at intervals of 0.02 kg m<sup>-3</sup>. Adapted from Yu et al. (2019b).

(2020) analyzed a tracer release experiment conducted in the Gulf Stream during a period with strong wind forcing and near-inertial oscillations. The observations and numerical simulations suggest that circulation associated with SI mixed the dye along isopycnals. This, combined with episodic vertical mixing associated

- with near-inertial shear led to significant cross-front mixing of the tracer due to shear dispersion.
- A global view of the scale and relative likelihood of SI, as computed by Dong et al. (2021), is provided in Fig. 8.6. The most unstable wavelength for SI ( $L_{SI}$ ) is estimated from Stone (1966)'s linear prediction applied to the upper ocean state extracted from the global submesoscale-permitting LLC4320 simulation. The SI scale varies strongly with latitude, with median values of 1.5 km at the equator to 15 m at high latitudes. It also varies with seasons as the median scale
- <sup>575</sup> roughly doubles in winter compared to summer. The SI scales are 1 or 2 orders of magnitude smaller than the MLI scale, and basin or global-scale models do not yet have sufficient resolution to capture SI.

#### 8.2.3 Submesoscale processes at the bottom of the ocean

Fronts can also form at the bottom of the ocean. This has been widely studied for
<sup>580</sup> application in coastal areas. For example, over a continental shelf, the alongshore winds in the presence of a cross-shelf density gradient can create upwelling or downwelling situations. In the upwelling case, which has been the most studied (Barth, 1989a,b, 1994; Durski and Allen, 2005), the surface front leads to the same type of baroclinic instability or symmetric instability as described
<sup>585</sup> previously. However, in the case of downwelling, a density front intersects the

bottom rather than the surface. This can lead to baroclinic instability as well, generating an eddy field with the same typical scale (1 - 10 km) (Brink, 2016).

Submesoscale currents and fronts are also found in deeper parts of the ocean, especially in the presence of steep topography such as seamounts and ridges. For example, energetic submesoscale currents are visible near the Mid-Atlantic Ridge in Fig. 8.3. The corresponding kinetic energy spectra exhibit a shallow  $\sim k^{-2}$  slope, contrasting with open-ocean – i.e., far from topographic features – regimes of turbulence, dominated by mesoscales and a  $\sim k^{-3}$  slope (Vic et al., 2018).

The bottom boundary layer (BBL) of the ocean exhibits key similarities with the surface boundary layer. Available potential energy associated with horizontal buoyancy gradients in the BBL can feed an equivalent of MLI (Wenegrat et al., 2018a). Friction and diapycnal mixing at the bottom can also inject or destroy PV in the BBL (Benthuysen and Thomas, 2012; Morel et al., 2019), which can
 either stabilize it or trigger a variety of unbalanced submesoscale instabilities like

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**FIGURE 8.10** Idealized depiction of various submesoscale processes in the bottom boundary layer. A boundary slope current moving in the direction of Kelvin wave propagation generates a downslope Ekman current. After loss of potential vorticity due to friction and diapycnal mixing at the bottom, the front can be unstable to gravitational instability (GI), symmetric instability (SI), or centrifugal instability (CI). Submesoscale eddies develop through baroclinic instability of the bottom mixed-layer (MLI). Schematic adapted from Naveira Garabato et al. (2019).

symmetric or centrifugal (inertial) <sup>8</sup> instabilities (Allen and Newberger, 1998; Molemaker et al., 2015; Dewar et al., 2015). The frictional drag can play the same role as the wind in the upper ocean and lead to forced instability regimes (Wenegrat and Thomas, 2020). Thus, most of the submesoscale instabilities

described in Section 8.2.2 in the surface layer have a counterpart at the bottom as summarized in Fig. 8.10 and described below.

### 8.2.3.1 Bottom boundary layer baroclinic instability

A counterpart to MLI occurs in weakly stratified boundary layers (Brink, 2012, 2013; Wenegrat et al., 2018a). The problem of baroclinic instability over a slope is a classic one (Blumsack and Gierasch, 1972; Mechoso, 1980; Solodoch et al., 2016), which has recently been revisited for buoyancy-driven flow by Hetland

<sup>8.</sup> Here we use the term 'centrifugal instability' synonymously with 'inertial instability' (as defined in Section 8.2.2.2) since the former has become the standard convention in studies of the BBL (McWilliams, 2016)



**FIGURE 8.11** Regime diagram for submesoscale baroclinic instability (MLI), symmetric instability (SI), centrifugal instability (CI), and mixed instability (SI/CI) in the ocean BBL as a function of the Richardson number  $Ri = N^2/u_z^2$  and the slope Burger number  $S = N\theta/f$ . The dashed red line shows the limit of zero PV, the dashed green line shows the limit of zero absolute vorticity  $f + \zeta = 0$ , and the dashed blue line is the theoretical expectation for the ratio of lateral and vertical shear production LSP/GSP = 1 in the hydrostatic limit. Adapted from Wenegrat et al. (2018a).

(2017) and for baroclinic instability over the continental shelf by Chen et al. (2020). It has also been used for low *Ri* regimes characteristics of the BBL by Wenegrat et al. (2018a).

The model is similar to the Eady model presented in Sec. 8.2.2.1, with the addition of a topographic slope  $\theta$ . The ratio of the topographic slope to minus the isopycnal slope is then given by the slope parameter:

$$\alpha = \frac{N^2}{fu_z}\theta = SRi^{\frac{1}{2}}$$
(8.18)

where:

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$$S = \frac{N\theta}{f} \tag{8.19}$$

<sup>620</sup> is the slope Burger number and *Ri* is the Richardson Number. As in Hetland (2017) and Wenegrat et al. (2018a),  $\alpha = 1$  corresponds to an isopycnal slope equal and opposite to the topographic slope and  $\alpha = -1$  to isopycnals parallel to the topography. With uniform background vertical stratification and slope-normal shear, the effect of the topographic slope is to stabilize baroclinic instability for  $\alpha < -1$  (Blumsack and Gierasch, 1972).

Realistic BBL structures have been shown to support submesoscale baroclinic instability (Wenegrat et al., 2018a). A first case corresponding to a BBL generated by bottom-intensified mixing supports a baroclinic instability that restratifies the thick outer layer of the BBL. A second case, corresponding to

an interior flow in the direction of Kelvin wave propagation (meaning that the flow has the coast on its right in the Northern Hemisphere), drives a downslope Ekman flow and generates available potential energy that also feeds a submesoscale baroclinic instability. In most BBL cases, the isopycnals intersect the bottom almost perpendicularly, corresponding to a positive  $\alpha$ , such that small positive values of  $\alpha$  and *S* might be the most common configuration in the BBL

(Wenegrat et al., 2018a).

The most unstable bottom MLI wavelength ( $L_{BMLI}$ , Fig. 8.6c,d) has also been estimated globally by Dong et al. (2020b), following the same methodology than for MLI in the surface layer (See section 8.2.2.1). The median values are in the order of O(1) km, thus slightly smaller than the surface MLI scales and well

into submesoscales.

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#### 8.2.3.2 Bottom injection of PV and submesoscale instabilities

Friction and diapycnal mixing at the bottom are strong sources of PV (Williams and Roussenov, 2003; Benthuysen and Thomas, 2012; Molemaker et al., 2015;

<sup>645</sup> Gula et al., 2015b). PV is extracted in the case of a boundary slope current moving in the direction of Kelvin wave propagation because the frictional drag reduces velocity along the slope, induces a negative horizontal velocity shear and a downslope Ekman flow that advects lighter water under denser water and drives diabatic mixing. PV is increased when the current is in the opposite direction

(meaning that the flow has the coast on its left in the Northern Hemisphere) when it leads to a positive horizontal velocity shear and an upslope Ekman advection that tends to restratify the bottom boundary layer (Benthuysen and Thomas, 2012).

The PV extraction related to downslope buoyancy advection is a close analogous of the PV extraction in the surface layer in the case of a downfront wind, as described in subsection 8.2.2.3. The advection of lighter water under denser water can generate convective mixing, which acts to increase the horizontal buoyancy gradient and decrease the vertical gradient, and can lead to a regime of forced SI or centrifugal (inertial) instability (CI) (Allen and Newberger, 1998;

Molemaker et al., 2015; Dewar et al., 2015; Jiao and Dewar, 2015; Gula et al., 2016; Yankovsky and Legg, 2018; Wenegrat et al., 2018a; Wenegrat and Thomas, 2020; Naveira Garabato et al., 2019).

As in the surface layer, these additional instabilities (GI, SI and CI/II) appear in the linear stability analysis of the Eady model when ageostrophic perturbations are included. The stability analysis for a geostrophically balanced along-slope flow in the direction of Kelvin wave propagation, with uniform stable stratification and uniform slope-normal velocity shear, is illustrated in Fig. 8.11 based on the scalings derived in Wenegrat et al. (2018a). When the slope Burger number is small, the criterion for instability is similar to that in the surface layer, namely SI is dominant for  $Ri \leq 1$  and MLI is dominant for  $Ri \gtrsim 1$ . When the slope

Burger number is increased, the dominant mode becomes CI or a mixed SI/CI mode at moderate Ri, and the baroclinic instability mode is shifted to larger Ri.

The different types of instabilities occurring when the PV is negative can be identified using the same criteria as in the surface layer (Sec. 8.2.2.2). In particular, instabilities can be classified based on their dominant source of energy: GI extract their energy predominantly from buoyancy flux (*BFLUX*), SI – from geostrophic shear production (*GSP*), and CI – from lateral shear production (*LSP*) terms. The limit between the CI and SI regimes in the stability diagram (Fig. 8.11) corresponds to the ratio of lateral and vertical shear production being equal to 1 (*LSP*/*GSP* = 1), which gives the condition  $\alpha = 1$  in the hydrostatic

limit (see Equ. 33 in Wenegrat et al., 2018a).

Recent high-resolution observations taken in an abyssal boundary current flowing along steep topography in the Orkney Passage highlighted the generation of GI, SI and CI in a configuration corresponding to a downslope Ekman flow

(Fig. 8.12, Naveira Garabato et al. 2019). GI is dominant in a  $\approx 100$  m thick layer over the bottom, while SI and CI happen over a larger region, which is about 1–2 km high and 500 m wide, as shown in Fig. 8.12. These instabilities generate an intensified near-boundary turbulence and drive buoyancy exchanges between the boundary layer and the interior.

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**FIGURE 8.12** Transect across an abyssal boundary current near the Orkney Passage sill (section B3 in Naveira Garabato et al. (2019)). (a) Along-slope velocity (color) and neutral density (in kg  $m^{-3}$ , black contours). (b) PV (color) and neutral density (black contours). (c) Instability type (color) and neutral density (black contours). Adapted from Naveira Garabato et al. (2019).

#### 8.2.3.3 Topographic wakes 690

A feature specific of the bottom is that, in the presence of a slope, it is possible for the highly sheared flow in the BBL to separate from the boundary and move into the stratified interior of the ocean, thus forming turbulent topographic wakes (Molemaker et al., 2015; Gula et al., 2015b, 2016), which can be even

more efficient at driving diapycnal mixing. If the boundary is horizontal, which 695 happens in the surface mixed-layer or over a flat bottom, the frictional drag can only induce a vertical velocity shear, such that the flow only acquires horizontal vorticity. It is thus unlikely to separate from the boundary as vertical motions are strongly limited by rotation and stratification, and instabilities and turbulence

- mostly stay inside the boundary layer (McWilliams, 2017). However, over a sloped bottom, the topographic drag induces both a vertical and a horizontal velocity shear, and the sheared layer has the capability of separating from the boundary either due to the geometry of the boundary (Molemaker et al., 2015) or due to the background mesoscale straining (Vic et al., 2015). Escaping the
- constraint of the boundary, the sheared flow undergoes instabilities such as CI/SI 705 or horizontal shear instabilities that lead to elevated local dissipation and mixing in the stratified interior (Gula et al., 2016) and to the generation of submesoscale coherent vortices (SCV) (Molemaker et al., 2015; Perfect et al., 2018; Srinivasan et al., 2019), which can further export tracers and water masses over much longer time and distances (Gula et al., 2019). 710

A typical case corresponds to a flow past a seamount, which may generate a turbulent topographic wake with both cyclonic and anticyclonic vorticity, leading to instabilities and formation of coherent vortices in the wake of the seamount, as seen from idealized (Perfect et al., 2018; Srinivasan et al., 2019) or realistic simulations (Srinivasan et al., 2017; Gula et al., 2019; Napolitano et al., 2021).

715 There are similarities with the more classical island wake, which forms as a von Karman street with alternating cyclones and anticyclones (Stegner, 2014).

Vorticity is similarly generated when a current flows along sloped topography. The vorticity may be cyclonic or anticyclonic depending on the orientation of the current relative to the topography. For example, the Gulf Stream along the U.S. 720 seaboard generates cyclonic vorticity. There, the topographic drag amplifies the horizontal cyclonic shear of the jet until the current separates from the slope. The highly sheared flow becomes unstable to barotropic shear instability, which leads to the formation of streets of submesoscale vortices as described in Gula et al. (2015a,b).

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The anticyclonic case is particularly interesting as it can trigger CI, which has a strong impact on energy dissipation and mixing (Dewar et al., 2015; Gula et al., 2016). Following the sequence of processes described in the context of the California Undercurrent (Molemaker et al., 2015) or the Gulf Stream (Gula

et al., 2016), relative vorticity can locally become much less than -f and result 730 in negative PV. The slope has a stabilizing effect upstream of separation, but the negative PV strip leads to intense CI and energy dissipation in the separated wake

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**FIGURE 8.13** Snapshots of potential vorticity (PV, in  $10^{-8} \text{ s}^{-3}$ ) along the Bahamas Banks showing generation of negative PV (in colors) along the slope and the onset of centrifugal instability in the wake. The big red arrow indicates the direction of the Gulf Stream, and the small black arrows the velocity vectors close to the slope. Density is shown in black contours with an interval of 0.5 kg m<sup>-3</sup> and along-slope velocity is shown in green contours with an interval of 0.2 m s<sup>-1</sup>. The inset on the right shows the instantaneous surface relative vorticity  $\zeta = v_x - u_y$ , normalized by f (in colors), with regions of high kinetic energy dissipation (depth-integrated energy dissipation  $\langle \epsilon \rangle > 2 \times 10^{-4}$  W m kg<sup>-1</sup>) highlighted in green. Adapted from Gula et al. (2016).

(see Fig. 8.13). In a Gulf Stream model, the vertically integrated dissipation rates of eddy kinetic energy due to parameterized turbulence (KPP), reach values up to  $8 \times 10^{-4}$  W m kg<sup>-1</sup> instantaneously at 26°N following separation of the negative PV strip from the slope. It is of the same order as the dissipation rates observed in an intense surface front within the Kuroshio Current (D'Asaro et al., 2011) integrated over the mixed-layer.

Equatorial topographic wakes are particularly efficient at dissipating energy (Srinivasan et al., 2021). The background rotation is important to drive the merging and alignment of vorticity structures in the wakes. However, in the tropics, the decreasing *f* leads to more vertically-sheared wake structures and increasing energy dissipation.

Topographic wakes are a common feature in realistic submesoscale-resolving simulations, and most of the studies on the subject come from idealized or realistic numerical simulations (McWilliams, 2016). It remains very complicated to sample such localized events of turbulence in the ocean, especially in the deep regions. Intense small-scale turbulence and the formation of submesoscale eddies have been observed in the wake of the Palau island chain, in the western

Pacific, during the program FLEAT (See articles in the special issue of Oceanography on the subject: Johnston et al., 2019; MacKinnon et al., 2019). Direct observations of turbulent wakes in the deep ocean are needed to better quantify the impact of theses processes. Deep seamounts and steep topographic features are numerous and the cumulative impact of topographic wakes on mixing might

<sup>755</sup> still be strongly underestimated.

# 8.2.4 The influence of vertical mixing on the evolution of a submesoscale front

In this section we will discuss the influence of small-scale turbulence and vertical mixing on the evolution of submesoscale fronts and thereby the submesoscale currents within. Study of these multi-scale interactions is at a relatively early stage and many open questions remain. Here, we discuss some of the advances that have been made in this area. We start by discussing the ageostrophic circulation in 'generalized Ekman' (GE) or 'turbulent thermal wind' (TTW) balance, driven by vertical mixing of momentum at fronts, emphasizing the connections between these balance relations. We then discuss the role that a GE/TTW balanced flow plays in the evolution of a front. Finally, we discuss the connection between GE/TTW balance and submesoscale instabilities.

As noted in Chapter 4, when averaged over a sufficiently long period of time, the wind-driven currents in a horizontally homogeneous mixed layer sufficiently far from the equator are expected to be in a state of turbulent Ekman balance,

(e.g., Cushman-Roisin and Beckers, 2011):

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$$-f\langle v^a \rangle = -\frac{d}{dz} \langle u'w' \rangle = \frac{d}{dz} \left( v_T(z) \frac{d \langle u^a \rangle}{dz} \right), \tag{8.20}$$

$$f\langle u^{a}\rangle = -\frac{d}{dz}\langle v'w'\rangle = \frac{d}{dz}\left(\nu_{T}(z)\frac{d\langle v^{a}\rangle}{dz}\right),$$
(8.21)

where superscript *a* denotes the ageostrophic velocity, angle brackets denote a time (and/or horizontal) average, and  $\nu_T$  is a turbulent viscosity which is assumed to be horizontally isotropic. The solution to these equations yields the classical Ekman spiral (Ekman, 1905), albeit modified by the depth-dependence of the turbulent viscosity. This balance has been confirmed with observations, although this requires a careful analysis and a long time average (Price et al., 1987; Lenn and Chereskin, 2009; Polton et al., 2013; Johnson et al., 2020a).

In classical turbulent Ekman balance, the geostrophic velocity (which was implicitly cancelled with the pressure gradient in Eqns. 8.20-8.21) is assumed to be depth-independent, and hence only the ageostrophic shear appears in the last term in each equation. At a front, however, the geostrophic flow also includes a vertical shear. The vertically-sheared geostrophic flow,  $\mathbf{u}_g(z)$ , can be mixed vertically by small-scale turbulence, thereby driving an ageostrophic response. In the context of wind-driven flow at fronts in the Tropical Pacific, Cronin and Kessler (2009) derived what they termed the 'generalized Ekman' balance, which can be written

$$-f\langle v \rangle = -\frac{1}{\rho_0} \left\langle \frac{\partial p}{\partial x} \right\rangle + \frac{d}{dz} \left( v_T(z) \frac{d\langle u \rangle}{dz} \right), \tag{8.22}$$

$$f\langle u\rangle = -\frac{1}{\rho_0} \left\langle \frac{\partial p}{\partial y} \right\rangle + \frac{d}{dz} \left( \nu_T(z) \frac{d\langle v \rangle}{dz} \right), \tag{8.23}$$

$$\frac{1}{\rho_0} \left\langle \frac{\partial p}{\partial z} \right\rangle = \langle b \rangle \,. \tag{8.24}$$

<sup>775</sup> Note that the full velocity,  $\mathbf{u} = \mathbf{u}_g + \mathbf{u}_a$ , appears in the Coriolis and vertical mixing terms. Wenegrat and McPhaden (2016) found analytical solutions to Eqns. 8.22-8.24 and extended the model to include the influence of surface waves, while Taylor and Ferrari (2010) found that this balance holds during forced symmetric instability (with the vertical momentum flux terms instead of a turbulent viscosity).

Alternatively, Eqns. 8.22-8.24 can be viewed as a generalization of thermal wind balance. Gula et al. (2014) note that when vertical mixing of momentum is included in a state that is otherwise in geostrophic and hydrostatic balance, the vertical shear satisfies the following equations



**FIGURE 8.14** Schematic of the cross-front turbulent thermal wind (TTW) circulation and its influence on the evolution of submesoscale fronts. Near the surface, convergent cross-front TTW circulation leads to frontogenesis as described in McWilliams et al. (2015); McWilliams (2017). Restratification by the TTW circulation and vertical mixing leads to frontolysis through shear-dispersion as described in Crowe and Taylor (2018, 2019).

$$-f\frac{d\langle v\rangle}{dz} = -\left(\frac{\partial b}{\partial x}\right) + \frac{\partial^2}{\partial z^2}\left(\nu_T \frac{\partial\langle u\rangle}{\partial z}\right),\tag{8.25}$$

$$f\frac{d\langle u\rangle}{dz} = -\left(\frac{\partial b}{\partial y}\right) + \frac{\partial^2}{\partial z^2}\left(v_T\frac{\partial\langle v\rangle}{\partial z}\right).$$
(8.26)

<sup>785</sup> Gula et al. (2014) called this 'turbulent thermal wind' (TTW) balance and they found that this described the circulation in simulations of submesoscale cold filaments in the Gulf Stream.

Note that Eqns. 8.25-8.26 can be obtained by taking the vertical derivative of Eqns. 8.22 and 8.23 and using 8.24. With a constant turbulent viscosity, <sup>790</sup> Charney (1973) showed that this is the leading order balance in the hydrostatic Boussinesq equations for small Rossby number and Crowe and Taylor (2018) showed that the same analysis can be extended to include a depth-dependent turbulent viscosity. Garrett and Loder (1981) and Ponte et al. (2013) discussed the use of Eqns. 8.25-8.26 to diagnose the circulation for given a density field

- <sup>795</sup> and  $v_T(z)$  and showed that simple solutions can be obtained in the limit of small Ekman number (i.e. weak vertical mixing) where the geostrophic shear can be used in the viscous terms. Finally, the dynamical balance underlying TTW is the same as the leading order balance in the subinertial mixed layer (SML) model of Young (1994).
- <sup>800</sup> Unlike the inviscid thermal wind balance, TTW balance is associated with a vertically-sheared cross-front flow. A simple explanation for this cross-front

flow is as follows. Consider starting with a front in thermal wind balance. Then, suppose that small-scale turbulence (*e.g.*, convection driven by surface cooling) leads to vertical mixing which reduces the along-front shear. Since the mixed layer depth is typically much smaller than the width of fronts, isotropic mixing by small-scale turbulence will not have a strong direct influence on the horizontal density gradient. As a result, the hydrostatic pressure gradient will also be relatively unaffected by small-scale mixing. Therefore, a reduction in the along-front shear by vertical mixing will lead to an unbalanced cross-front

Pressure gradient which will, in turn, drive a cross-front flow. The cross-front flow associated with this mechanism will always be in the sense to re-stratify the front with light water advected over dense water. The TTW circulation is also associated with a surface PV flux at submesoscale fronts which may dominate both wind and surface buoyancy-flux-driven PV fluxes. These effects have been shown to modify the seasonal cycle of mode water formation in the Gulf Stream

(Wenegrat et al., 2018b).

The cross-front GE/TTW flow can influence the evolution of the front and the associated submesoscale instabilities. This represents a mechanism whereby vertical mixing by small-scale turbulence can influence submesoscales (Garrett

- and Loder, 1981; Thompson, 2000). As discussed in Garrett and Loder (1981), the unbalanced pressure gradient and hence the cross-front flow will tend to be largest at the location where the horizontal density gradient is maximum and the cross-front flow will naturally tend to zero outside the front. As sketched in Figure 8.14, the horizontal convergence/divergence of the TTW circulation will
- lead to downwelling on the dense side of the front and upwelling on the light side of the front. Near the surface on the dense side of the front, the convergence of the TTW flow will lead to frontogenesis. McWilliams et al. (2015) and Sullivan and McWilliams (2018) show that this leads to a rapid collapse of outcropping dense filaments (where the TTW circulation consists of two counter-rotating
- cells with downwelling in the center of the dense filament). McWilliams (2017) developed a diagnostic framework which combined the TTW circulation with the Omega equation to analyze the secondary circulation and frontogenetic tendency for fronts and filaments. Bodner et al. (2019) used a perturbation approach to investigate the influence of horizontal and vertical mixing on the evolution of a
- <sup>835</sup> front based on the inviscid frontogenetic model described in Shakespeare and Taylor (2013). A diurnal modulation of the small-scale turbulence, driven by the solar cycle, has been shown to drive a diurnal modulation cycle of frontogenesis and relaxation (Dauhajre and McWilliams, 2018), which can be described using transient turbulent thermal wind (T3W) equations.
- As discussed in Garrett and Loder (1981), Young (1994), and Crowe and Taylor (2018), the vertically-sheared cross-front TTW circulation can cause the width of the front to increase through shear dispersion (*e.g.*, Young and Jones, 1991). As the cross-front circulation slumps the isopycnals, small-scale turbulence mixes density vertically, and the sustained combination of these two
- processes leads to an increase in the frontal width and a spindown of the front.

When the turbulent viscosity depends only on z, Crowe and Taylor (2018) found that surface-intensified frontogenesis occurs during a brief transient phase before the front spreads through shear dispersion. They also found that as the front spreads, it limits to a self-similar shape with a roughly constant horizontal density gradient in the interior of the front. At the edges of the front, intense narrow bands of upwelling and downwelling appear in analytical solutions (Crowe and

Taylor, 2018) and numerical simulations (Crowe and Taylor, 2018). Crowe and Taylor (2020) extended this work to include the circulation driven by a surface wind stress and a surface buoyancy flux and identified the conditions when the front sharpens or spreads.

Most of the studies referenced above represent vertical mixing using a prescribed turbulent viscosity (*e.g.*, Crowe and Taylor, 2018), a simple model for mixing (*e.g.*, Young, 1994), or a boundary layer parameterization (such as the KPP scheme) (*e.g.*, Gula et al., 2014; McWilliams et al., 2015). Although

- large-eddy simulations have shown that turbulent mixing can be significantly modified at submesoscale fronts (*e.g.*, Taylor, 2016; Smith et al., 2016), much less is understood about how turbulence reacts and couples with the evolution of submesoscale fronts. One notable exception is Sullivan and McWilliams (2018) who studied large-eddy simulations of a collapsing submesoscale cold
- <sup>6865</sup> filament. Small-scale turbulence was generated in their simulations by wind forcing and/or surface cooling. Turbulence triggered the collapse of the filament through GE/TTW-induced frontogenesis. However, in the later stages of the filament evolution, this frontogenesis is arrested by enhanced turbulence generated through horizontal shear instabilities, as further discussed in Sec. 8.2.5.
- <sup>870</sup> There are many open questions related to the interactions between submesoscale fronts and turbulent mixing. For example: Does the suppression of vertical mixing following frontal re-stratification (Taylor and Ferrari, 2011) enhance or inhibit TTW-induced frontogenesis? How is the spreading of a front by sheardispersion changed when turbulence is modified by frontal shear/stratification?
- <sup>875</sup> What factors influence the arrest of frontogenesis by turbulence and hence equilibrium frontal widths? One of the major challenges in this area is the computational cost associated with simulations that capture both changes to small-scale turbulence and the evolution of submesoscale fronts. For example, the simulations in Sullivan and McWilliams (2018) used  $\sim 10^{10}$  grid points. However,
- advances in computing power should make these simulations more accessible, and will allow an exploration of parameter space that will likely be necessary to develop and test parameterizations of these processes.

#### 8.2.5 Frontal arrest and routes to dissipation

The theory of frontogenesis does not explain how the sharpening of the front is <sup>885</sup> ultimately stopped. As noted above, inviscid theory predicts the formation of a discontinuity in the surface density in a finite time (Hoskins and Bretherton, 1972). In reality the sharpening of the front can be arrested due to spatio-

temporal variability of the large-scale flow (McWilliams et al., 2019), dissipation by intensified small-scale turbulence or an instability and eddy-feedback
equilibration process. Frontal arrest due to the effect of baroclinic instability has been shown in McWilliams and Molemaker (2011). Another likely scenario is the triggering of horizontal shear instability (Gula et al., 2014; Samelson and Skyllingstad, 2016; Sullivan and McWilliams, 2018; Verma et al., 2019), which has growth rates scaling with the cross-front velocity gradient. This scenario for

- <sup>895</sup> frontal arrest has been confirmed using large-eddy simulations of an idealized dense filament by Sullivan and McWilliams (2018). Within less than a day, frontogenesis is arrested at a small width ( $\approx 100$  m), primarily by an enhancement of the turbulence through a small submesoscale, horizontal shear instability of the sharpened filament, followed by a subsequent slow decay of the filament by
- further turbulent mixing. However, other studies have found sharpening of a front down to O(10) m until the release of a gravity current (Pham and Sarkar, 2018).

Submesoscale processes can thus initiate a forward cascade of energy and tracer variance, ultimately leading to energy dissipation and diapycnal mixing in frontal regions. Evidence of such a forward cascade of energy to dissipative scales has been observed at isolated small-scale frontal features in idealized high-resolution numerical simulations of MLI (Molemaker et al., 2010; Skyllingstad and Samelson, 2012; Samelson and Skyllingstad, 2016). Quanti-

- tative assessments in submesoscale-permitting realistic model have confirmed that the forward cascade of kinetic energy at the smallest resolved scales of the models occurs mainly in frontogenetic regions (Schubert et al., 2020), and that superinertial ageostrophic motions play an important role (Ajayi et al., 2021). However, the submesoscale energy cascades have also been shown to be strongly time and region dependent (Yang et al., 2021).
- <sup>915</sup> Very high levels of turbulent kinetic energy dissipation have been observed at strong persistent fronts like the Kuroshio or Gulf Stream (Nagai et al., 2009; D'Asaro et al., 2011; Nagai et al., 2012). In the open-ocean, on the other hand, the contribution of submesoscale processes to small-scale turbulence may seem weak compared to the contribution of winds and waves, as observed during the
- 920 OSMOSIS campaign (Buckingham et al., 2019), but they still have an important impact for extracting energy from the geostrophic circulation. Observations of a front in the Baltic Sea, following the passage of a storm, have also highlighted a direct route to turbulent dissipation, linked to shear instability (Carpenter et al., 2020). Another observation of a density filament in the Benguela upwelling
- system also confirmed high level of energy dissipation driven by forced SI (Peng et al., 2020).

# 8.3 REDISTRIBUTION OF DENSITY AND RESTRATIFICATION AT THE SUBMESOSCALE

Submesoscale instabilities tend to reduce horizontal density gradients and enhance vertical density gradients – i.e., they are restratifying in nature. The reason is twofold: Some of these instabilities tap into the available potential energy associated with lateral density gradients directly, while others draw kinetic energy from currents, disrupt the thermal wind balance, and force the lateral gradients to adjust. This results in ageostrophic secondary circulations that act to restratify

the flow on time scales of hours to weeks. The stratification of the upper-ocean is thus controlled by the competing effects of vertical mixing and restratification. The relative importance of these two processes is important in determining the density structure of the upper ocean.

In this section, we first describe separately the effect of the different sub-<sup>940</sup>mesoscale processes presented in Sec. 8.2 on the restratification of the ocean. Then, we comment on the competition between the different type of processes and their overall importance in the ocean.

#### 8.3.1 Restratification induced by submesoscale processes

Submesoscale processes can increase vertical stratification on time scales that <sup>945</sup> compete with surface radiative forcing. Submesoscale restratification is usually quantified in terms of the horizontal u'b' or vertical buoyancy flux w'b', which correspond to a redistribution of density, but are often expressed as an equivalent surface heat flux to facilitate comparison with the ubiquitous restratification due to surface heat fluxes and freshwater input.

- Earlier works on submesoscale frontal slumping have highlighted the role of geostrophic adjustment (Tandon and Garrett, 1994) and of the ASC associated with surface frontogenesis (Lapeyre et al., 2006) to restratify the horizontal gradients generated by wind mixing and the straining of mesoscale eddies. In this case, the vertical buoyancy flux associated with strain-induced frontogenesis
- of a single front scales as  $w'b' \sim H^2 |\nabla_h b| / f^2$  (McWilliams, 2016), where *H* is the mixed layer depth, and  $\nabla_h b$  is the horizontal buoyancy gradient at the front.

During SI, restratification occurs primarily via a horizontal buoyancy flux associated with the vertically-sheared cross-front flow (Taylor and Ferrari, 2010). Bachman et al. (2017a) proposed a parameterization for restratification by SI.

Since SI is generally faster than MLI, in an initial value problem (or following a sudden forcing event) SI typically acts in the early stages of the response before transitioning to MLI (Stamper and Taylor, 2017). In the idealized experiments of Fox-Kemper et al. (2008), SI brings the front to Ri = 1, *i.e.*,  $N^2 = |\nabla_h b|^2 / f^2$ , then MLI becomes the primary instability process. The complementary roles of

SI and MLI are illustrated by the simulations of frontal regions under destabilizing heat forcing in Taylor and Ferrari (2011): restratification occurs very rapidly (less than a day) due to SI whereas MLI achieves a much stronger restratification but on much longer times (several days). In Verma et al. (2019) as well, during the spindown of a front, the initial configuration with Ri = 0.26 is unstable to SI

970 that then develops secondary KH instability and three-dimensional turbulence. The MLI soon becomes the dominant mode as Ri increases to beyond 0.95 during restratification of the front.

Restratification driven by finite-amplitude MLI is an adiabatic process that <sup>975</sup> can be represented through advection by an eddy-driven overturning streamfunction (Boccaletti et al., 2007; Fox-Kemper et al., 2008):

$$\Psi^* \sim -C_e \frac{H^2 |\nabla_h b|}{f} \tag{8.27}$$

and an associated buoyancy flux:

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$$\overline{w'b'} \sim C_e \frac{H^2 |\nabla_h b|^2}{f},\tag{8.28}$$

with  $C_e \approx 0.06$  determined from idealized experiments by Fox-Kemper et al. (2008). A parameterization of MLI restratification effects has been developed by

- Fox-Kemper et al. (2008); Fox-Kemper and Ferrari (2008) based on this scaling, analogously to what was done by Gent and Mcwilliams (1990) to parameterize interior baroclinic instability for non-eddying ocean models. This parameterization contributed to improve the properties of the mixed-layer in climate models (Fox-Kemper et al., 2011; Gent et al., 2011). For example, it can reduce the
- maximum mixed-layer depth by up to 200 m in the Southern Ocean and correct systematic biases with important climatic impacts (Calvert et al., 2020). However it was also noted by Callies and Ferrari (2018b) that this scaling only represents the initial phase of the instability, but is not valid anymore when MLI reaches the finite-amplitude stage and develop larger eddies and stronger velocities than
- assumed in the scalings. In the numerical experiments of Capet et al. (2008b), for example, the submesoscale vertical buoyancy flux due predominantly to MLI is ~ 100 W m<sup>-2</sup>, exceeding the prediction of Eq. 8.28. Note, however, that the rate of restratification by MLI may be impacted by the parameterization of vertical eddy viscosity in a given model (Mukherjee et al., 2016).

# 8.3.2 Competition between destratification and restratification of a front

The two main factors driving turbulence in the mixed layer are the surface buoyancy flux and wind. When the horizontal density gradient is sufficiently weak, surface cooling (corresponding to a surface buoyancy flux  $B_0 > 0$ ) will drive mixing and destratification through convection. Wind blowing over a front may restratify the mixed layer if the wind is blowing upfront (and advecting light water over dense water) or destratify if the wind is blowing downfront (and advecting dense water over light water). As discussed in subsection 8.2.2.3, the wind drives an Ekman buoyancy flux (EBF) that scales as:

$$\text{EBF} \sim \tau_w^a \frac{|\nabla_h b|}{\rho f},\tag{8.29}$$

- where  $\tau_w^a$  is the along-front wind stress. Note however that, even though the relative orientation of fronts and winds is nearly isotropic on a global scale, there is an asymmetry in the processes leading to a larger upwind restratification than downfront destratification for an equal wind stress (Thomas and Ferrari, 2008).
- In the presence of wind forcing, the impact of the submesoscale processes on restratification can be different than the picture drawn in the previous subsection. Depending on the relative strengths of the wind-driven Ekman flow and the frontal ASC, wind-driven destratification can overcome restratification induced by the ASC related to frontogenesis (Thomas and Ferrari, 2008). The competition between destratification by downfront winds and restratification by

<sup>1015</sup> MLI has been studied by Mahadevan et al. (2010). The relative importance of the destratification by down-front winds compared to the restratification by MLI can be characterized by a ratio between the respective buoyancy fluxes. Using Eq. 8.29 and Eq. 8.28, this ratio is:

$$R = \frac{\tau_w^a}{C_e H^2 \rho |\nabla_h b|}.$$
(8.30)

In the simulations of Mahadevan et al. (2010), the ratio is equal to 1 and the restratification by MLI is countered by a down-front wind stress  $\tau_w \approx 0.2$  N m<sup>-1</sup>. However, the amplitude of the destratifying buoyancy flux diminishes with time as the alignment between the wind and front is disrupted by the growth of the frontal instability.

- <sup>1025</sup> MLI is relatively resilient to convective mixing and found to grow in most conditions. MLI shuts off convection in conditions of weak buoyancy forcing (Mahadevan et al., 2010). MLI is also active and capable of generating submesoscale eddies in the presence of strong convection even if it is unable to completely restratify the flow and shut off convection (Callies and Ferrari,
- <sup>1030</sup> 2018a). The convective deepening of the mixed-layer is partially balanced by the submesoscale buoyancy flux due to MLI, leading to a more heterogeneous and shallower mixed-layer than would be the case in the absence of submesoscales (Couvelard et al., 2015). A similar resilience of MLI-driven restratification was observed during the passage of an intense idealized autumn storm by Whitt and
- Taylor (2017). Despite the strong destratifying effect due to downfront winds, the submesoscales intensified during the storm and maintained a strong stratification in local patches. Considering a balance between MLI and the effect of a fixed vertical diffusion would imply a restratification rate one order of magnitude larger than Eq. 8.28 (Bachman and Taylor, 2016). In a more realistic situation,

<sup>1040</sup> based on a submesoscale-resolving simulation of the central part of the Baltic Sea, Chrysagi et al. (2021) confirmed that submesoscales are able to maintain shallow mixed-layer depths in local patches during the passage of storms and that a rapid restratification is at work after the passage of the storms. This submesoscale restratifying effect has important implications because the mixing <sup>1045</sup> efficiency can remain high ( $\Gamma = 0.2$ ) at submesoscale fronts, contrary to regions where the mixed-layer is already well-mixed (Chrysagi et al., 2021).

Global estimates using Argo profiling float observations highlight the importance of MLI to the restratification of the upper ocean (Johnson et al., 2016). The mechanism is particularly effective in the regions and times where the mixed-

- <sup>1050</sup> layer is deep, in particular during the transition from winter to spring when the mixed-layer is at its deepest. Regions of deep convection (Haine and Marshall, 1999) and inside anticyclones (Bosse et al., 2019) are also characterized by enhanced MLI-driven restratification. A number of in-situ observations have confirmed the importance of the MLI-driven restratification around the globe: *e.g.*, in the north-east Pacific (Hosegood et al., 2006), in the Southern ocean (Bachman et al., 2017b; du Plessis et al., 2017), or in the Antarctic Marginal Ice Zone and under sea ice, where the equivalent heat flux can reach ~ 240 W m<sup>-2</sup> in mid-winter (Biddle and Swart, 2020). However, the few high-resolution observations at individual fronts, like the ones taken along the rim of a South-
- ern Ocean mesoscale eddy (Adams et al., 2017) or over a California Current upwelling front (Johnson et al., 2020a,b), are also exposing that the destratification/restratification of the front is often complex and involve interactions between many processes.
- Observations of submesoscale fronts over long periods are very difficult to obtain, and the Ocean Surface Mixing, Ocean Submesoscale Interaction Study (OSMOSIS), which took place in the north-east Atlantic, is one rare example. The year-long records of in-situ measurements from a glider and a mooring array highlight a strong seasonal cycle of submesoscale turbulence (Buckingham et al., 2016) with several instabilities controlling the stratification of the upper ocean: The mixed-layer deepens in the fall due to GI, and is restratified by SI and MLI throughout the winter (Thompson et al., 2016; Yu et al., 2019b).

Year-long observations were also obtained with a similar mooring array in the North Pacific Subtropical Countercurrent during the SubMESI experiment (Zhang et al., 2020). The SubMESI mooring was located in a region more typical of subtropical gyres with a shallower mixed-layer and higher eddy kinetic energy than the north-east Atlantic. Submesoscale turbulence is driven there by a combination of MLI and strain-induced frontogenesis leading to an equivalent upward heat flux comparable in magnitude with the net surface heat fluxes during late winter and early spring.

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Submesoscale processes play an important role in the surface mixed-layer, but it remains unclear how effectively they can penetrate into the underlying pycnocline and significantly contribute to vertical heat and buoyancy fluxes in the interior. Intense frontogenetic regions with ageostrophic dynamics are present in the ocean interior in the idealized simulations of Molemaker et al. (2010) and Barkan et al. (2015). However, the dynamical regimes in these simulations are characterized by a large  $M^2/N^2$  ratio (= 0.2 in Molemaker et al. (2010)) compared to typical interior ocean values (see discussion in Capet et al. (2016)).

Examples of submesoscale fronts that penetrate below the mixed layer have been documented by Yu et al. (2019a); Zhang et al. (2020). Recent observations and modelling in the Southern Ocean have highlighted the presence of deep submesoscale fronts reaching down to 1000 m depth. These fronts are generated by the straining associated with Southern ocean mesoscale eddies and are associated with active frontogenesis. They drive an anomalous upward heat transport

- from the ocean interior to the surface that acts to restratify the ocean interior (Siegelman et al., 2020; Siegelman, 2020). Similar deep reaching fronts might be present in regions with strong horizontal gradients (*e.g.*, western boundary currents and regions with intense mesoscale activity) and low stratification (*e.g.*, high latitudes regions). The submesoscale vertical heat transport computed at
- <sup>1100</sup> 200 m depth by Su et al. (2018, their Fig. 3c,d) might give a good idea of where to expect such deep reaching fronts.

#### 8.3.3 Bottom boundary layer mixing and restratification

In the BBL, unbalanced submesoscale processes linked to negative PV (GI, CI, SI) can produce small-scale turbulence and contribute to mixing the fluid toward a state of marginal stability. Recent observations by Ruan et al. (2017) in the southern Drake Passage have highlighted the presence of strong lateral buoy-

- ancy gradients along slopes and enhanced bottom turbulence associated with submesoscale instabilities, leading to thick bottom mixed layers and water-mass modifications. Observations in the Orkney passage, shown in Fig. 8.12, have also highlighted a vigorous turbulent mixing associated with submesoscale instabilities, in particular CI and SI (Naveira Garabato et al., 2019). Microstructure
- measurements revealed turbulent dissipation and mixing rates exceeding oceanic background values by one to three orders of magnitude in the abyssal boundary current. However, to maintain efficient water-mass transformations, it is also essential that the mixed waters are exported out of the mixed-layer and replaced by stratified waters from the interior. These instabilities also drive such lateral
- by stratified waters from the interior. These instabilities also drive such lateral exchanges (Naveira Garabato et al., 2019), leading to a high mixing efficiency (0.6 1) compared to a typical efficiency of 0.2 (Spingys et al., 2021).

The contribution of topographic wakes to mixing may also be significant as the mixing efficiency of CI is particularly high in the stratified interior (Dewar et al., 2015; Jiao and Dewar, 2015; Gula et al., 2016). In the idealized numerical experiments of Perfect et al. (2020), large volume-averaged diapycnal diffusivities are found in the wake of a seamount. They are shown to scale like the product of the Froude and Rossby numbers squared :  $K_{rho} \sim (Fr Ro)^2 = (\frac{U}{NH} \frac{U}{fD})^2$ , where *H* and *D* are the height and half-width of the seamount.

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Similarly to the surface, bottom MLI draws energy through the vertical buoyancy flux and contributes to a restratification of the bottom mixed layer (w'b' > 0). MLI is thus suspected to directly affect the strength and structure of the abyssal overturning circulation by playing a crucial role to balance the effect of bottom-intensified mixing and allow for sustained water mass transformations (Callies, 2018), see also chapter 3 and 7. The stratification over the flanks of mid-ocean ridge systems seem to be largely maintained by submesoscale baroclinic eddies, contrary to the stratification within ridge-flank canyons, which is maintained by mixing-driven mean flows (Ruan and Callies, 2020).

# 1135 8.4 REDISTRIBUTION OF PASSIVE TRACERS AND PARTICLES

In this section, we describe the role of submesoscale processes in redistributing *passive* ocean tracers (those that do not affect the density of sea water). We consider two kinds of passive tracers: Firstly, those that are *conservative*, i.e. have no interior sources and sinks, and hence affected only by boundary fluxes, physical transport, and mixing. Secondly, those that are *reactive*, i.e. altered by growth and decay processes. Naturally most biogeochemical tracers are regarded as reactive, since they are affected by biological growth or decay that occurs in the presence of another variable or property, such as photosynthesis in the sunlit region.

- The same tracers may exhibit different active/passive or conservative/reactive behaviors depending on the situation. For example, temperature and salinity affect the density of sea water and therefore are undeniably active. However, most currents in the ocean are isopycnal, even at the submesoscales. When such motions are considered, temperature or salinity anomalies act as *passive* tracers that are stirred on isopycnal surfaces by the eddying flow field. Density-
- compensated thermohaline variability is often the most convenient passive tracer to study, since it is found ubiquitously in the world's oceans even where other passive tracers may be absent.
- Discrete particulate matter suspended in the ocean (such as plankton, larvae, sediment, microplastics, oil droplets, etc.) as well as macroscopic objects (marine debris, kelp, ice floes) often behave similarly to passive tracers, although their redistribution is additionally complicated by the buoyancy and inertia effects.

#### 8.4.1 Conservative tracers

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<sup>1160</sup> Conservative passive tracers in the ocean are stirred by the eddying flow field, creating tracer variability over a range of scales. This variability can be characterized by an isopycnal spectrum of a tracer variance P(k), where k is the horizontal wave number. The passive tracer spectrum is theoretically predicted to be universally related to the stirring eddy flow field and its turbulent kinetic energy spectrum E(k), at least for well developed turbulence (Vallis, 2006): For a uniformly rolling-off kinetic energy spectrum  $E(k) \sim k^{-n}$ , n < 3, the corresponding conservative passive tracer variance spectrum rolls off as

$$P(k) \sim k^{(n-5)/2}$$
. (8.31)

In the interior ocean, quasi-geostrophic dynamics suggests that  $E(k) \sim k^{-3}$ , corresponding to the tracer variance spectrum  $P(k) \sim k^{-1}$ . On the other hand, surface-quasigeostrophic theory applicable to near-surface submesoscale processes produces kinetic energy and passive tracer spectra with the same slope, *i.e.*,  $E(k) \sim P(k) \sim k^{-5/3}$ . Relationship (8.31) breaks down for steep kinetic energy spectra (n > 3), where stirring becomes non-local and  $P(k) \sim k^{-1}$ (Batchelor, 1959). As (8.31) suggests, when smaller scale turbulence is more energetic (the E(k) spectrum is flatter) there is more vigorous stirring of passive tracers, resulting in less tracer variance at smaller scales and a steeper tracer variance spectrum P(k) (Scott 2006; Callies and Ferrari 2013; Lagrer et al

variance spectrum, P(k) (Scott, 2006; Callies and Ferrari, 2013; Jaeger et al., 2020a). A number of observational studies have tried to analyze the spectra of passive

tracers in the pycnocline, but until recently, they lacked the horizontal resolution to conclusively measure the spectrum at submesoscales. A major oceanographic field experiment called LatMix (Scalable Lateral Mixing and Coherent Turbulence, Shcherbina et al., 2015), aimed at observing submesoscale stirring, was conducted in 2012 in the northwestern Atlantic. Direct measurements of dye dispersion highlighted stirring by submesoscale eddies (Sundermeyer et al.,

2014). Spectra of salinity anomalies along isopycnals, which behave mostly like a passive tracer, pointed to a steeper variance at submesoscale than expected from (surface) quasi-geostrophic motions (Kunze et al., 2015), consistent with other sets of observations (Klymak et al., 2015). Another recent study (Jaeger

- et al., 2020b) that compiled 4,800 km of ship track with underway-CTD profiles at spacings of 0.3–3 km in the Bay of Bengal, also showed a steepening of the tracer variance spectrum at submesoscales, suggesting that submesoscales are acting to mix tracers along isopycnal surfaces in the pycnocline. Submesoscale streamers were also observed during the LatMix experiment. They were asso-
- ciated with a significant freshwater flux across the sharp north wall of the Gulf Stream (Klymak et al., 2016), which was previously considered as a barrier to lateral mixing. These exchanges across the Gulf Stream front have been further characterised using dye observations and numerical simulations as a result of a combination of strong vertical mixing events and shear dispersion induced by submesoscale instabilities (Wenegrat et al., 2020).

Submesoscale isopycnal stirring appears to vary strongly across isopycnals, creating complex vertical interleaving of water masses (Shcherbina et al., 2009; Jaeger et al., 2020a). Interleaving layers can be 1–10 m thick, tens of kilometers in horizontal extent, and tends to be tilted with respect to the isopycnals. These interleaving intrusions of water are generated by the swirling flow associated with eddies, both at mesoscales (Smith and Ferrari, 2009) and submesoscales. The submesoscale signatures suggest that the vertical shear of the horizontal ve-

locity, which is associated with the strong lateral density gradients in the mixed layer, is critical for generating layers in water mass anomaly that are tilted with respect to the isopycnal surfaces (Jaeger et al., 2020a). The very thin (depth to length) aspect ratio of the layers creates a strong vertical gradient in the tracers, which is then smoothed through diapycnal mixing. In this way, lateral stirring by submesoscale processes creates thin layers with sharp vertical gradients that result in enhanced diapycnal mixing.

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#### 8.4.2 Mixing and transport of reactive tracers

Along-isopycnal vertical transport is associated with isopycnal stirring, which becomes more efficient with submesoscale dynamics. This is why submesoscale processes are responsible for enhancing the vertical transport of biogeochemical tracers such as nutrients, carbon and oxygen (Thomas et al., 2008). The net 1220 vertical flux of a biogeochemical tracer is the integral of w c', where c' is the tracer anomaly from the tracer mean at that depth. Hence, the flux depends on the covariance of the vertical velocity and tracer anomaly, and is dependent on the relative timescales for the biogeochemical reaction (or modification) and vertical transport. This is one of the reasons that submesoscale vertical velocities 1225 are efficient in transporting biogeochemical properties (Whitt et al., 2019).

Model simulations have shown that increasing horizontal grid resolution leads to a greater vertical supply of nutrients (Lévy et al., 2012; Uchida et al., 2020) and stronger tracer subduction into the pycnocline (Balwada et al., 2018).

A careful analysis (Freilich and Mahadevan, 2019) shows that although the 1230 vertical uplift of isopycnals is the larger component of vertical transport, the along-isopycnal component of vertical transport is more sensitive to model resolution and accounts for a larger fraction of vertical flux when the submesoscale activity is increased.

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#### 8.4.3 Impacts on the dispersion of buoyant material

Surface submesoscale currents can produce strong local dispersion (spreading) of passive tracers down to 100 m scales with implications for the predictive modeling of oceanic pollutants (Poje et al., 2014). At the same time, frontogenetic submesoscale flows are characterized by zones of sharp convergences of hori-1240 zontal currents at the ocean surface (see discussion in Section 8.2.1), which are naturally anti-dispersive. Convergence zones concentrate buoyant material, such as plankton, natural surfactants, pollutants (particularly, oil and oil degradation products), and marine debris. Highly buoyant material remains close to the surface, therefore breaking the three-dimensional non-divergence, and allowing

1245 strong accumulation within convergence zones (D'Asaro et al., 2018).

Taylor (2018) used large-eddy simulations of MLI under various intensities of convective forcing to study the influence of submesoscales on buoyant tracers. When the buoyant rise velocity was not small compared to the *rms* vertical fluid velocity, the buoyancy tracers accumulate near the surface in a submesoscale front that wraps around the submesocale eddy, mirroring the patterns seen in observations (D'Asaro et al., 2018). Intense downwelling at the submesoscale front pulls the buoyant tracers beneath the surface. In some cases this results in the buoyant tracer extending deeper into the water column than it would in the absence of submesoscales.

#### 8.4.4 Dispersion by the deep submesoscale currents

Submesoscale currents also contribute to the dispersion and transport of passive tracers at the bottom and in the interior of the ocean. Submesoscale currents (as well as tidal currents) generate significant horizontal and vertical dispersion of tracers close to the topography. For example, over the Mid-Atlantic ridge, submesoscale currents have been shown to influence dispersion of deep-sea hydrothermal vents effluents and larvae and impact connectivity between deep-sea ecosystems (Vic et al., 2018).

Deep submesoscale currents can also generate long-range anomalous transport of tracers in the ocean interior in the form of subsurface submesoscale eddies, known as Submesoscale Coherent Vortices (SCVs) (McWilliams, 1985) or Intra Thermocline Eddies (ITEs) (Dugan et al., 1982). SCVs are usually defined as energetic eddies with a radius smaller than the Rossby deformation radius, a structure localized in the vertical, and an interior velocity maximum

(McWilliams, 1985). SCVs may be generated due to various frictional or diabatic effects, which include: convection (Marshall and Schott, 1999), winddriven destruction of PV (Thomas, 2008), geothermal forcing (Baker et al., 1987), bottom mixing (McWilliams, 1985), or friction (D'Asaro, 1988), or by inviscid instability processes of bottom currents such as baroclinic instability (Morvan et al., 2019). Topographic wakes are suspected to be the major source

of SCVs (McWilliams, 2016).

SCVs can be very long-lived (> 1 year) and travel far from their origins, being primarily advected by mesoscale and mean currents. One of the most well-known types of SCVs are Meddies (even if they are formally closer to mesoscale than submesoscale) formed at the exit of the Mediterranean Sea (McDowell and Rossby, 1978), which spread salty Mediterranean waters in the subtropical Atlantic ocean. SCVs that form in eastern boundary regions are

essential for spreading oxygen-poor and nutrient-rich waters into the interior of gyres (Frenger et al., 2018). SCVs also form from wintertime deep convection, as observed in the Labrador Sea (Clarke, 1984; Lilly and Rhines, 2002) and the

northwestern Mediterranean Sea (Testor and Gascard, 2003; Bosse et al., 2016, 2017) where they are essential for spreading the newly formed deep waters within ocean basins. SCVs formed in the wake of topographic features, for example

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the Charleston Bump along the U.S. seaboard, can transport waters from the bottom mixed layer over long distances and spread them within the subtropical gyre (Gula et al., 2019).

SCVs have always been very difficult to sample due to the sparsity of in situ observations able to resolve submesoscales in the interior of the ocean. Thanks to the coverage of Argo floats, it is now possible to make more robust statistics

on the existence and properties of the SCVs (Li et al., 2017; McCoy et al., 2020). The cumulative effect of SCVs could potentially affect the large-scale transport and distribution of heat, nutrients, and biogeochemical tracers. However, a quantitative assessment of such impacts still remains to be done.

### 8.5 CONCLUSION AND FUTURE DIRECTIONS

- As an intermediary between balanced flows and small-scale turbulence, submesoscales play an important part in the story of ocean mixing. Through the instabilities described in sections 8.2.2 and 8.2.3, submesoscales restratify the surface and bottom mixed layers (see section 8.3), while turbulent mixing influences the evolution of submesoscale fronts by generating a cross-front circulation
- as described in section 8.2.4. At the same time, submesoscales drive strong vertical circulations that re-distribute passive, active, reactive, and buoyant tracers while stirring tracers along isopycnals, transporting material through the ocean interior and shortening the route to small-scale mixing (section 8.4).
- The body of knowledge on submesoscale processes has grown substantially over the last 15 years. However, many theoretical and modelling studies have 1310 considered only a subset of the submesoscale processes mentioned here - either by design or by limitations in resolution. The multi-scale interactions between various processes (e.g., boundary layer turbulence, SI, MLI, internal waves, and mesoscale eddies) remains relatively unexplored. Recent advances in computational power have made it possible to begin to study at least some of these 1315 interactions. For example, Skyllingstad and Samelson (2020) used large-eddy simulations to study the interaction between boundary layer turbulence, SI, and MLI, while submesoscale-permitting global ocean models (e.g., Su et al., 2018, 2020) have provided insight into the influence of submesoscales on large-scale circulation and heat transport. Piecing together the links between small-scale 1320 turbulence and mixing, submesoscales, mesoscale eddies, internal waves and the general circulation remains a grand challenge.

The effect of air-sea coupling at the submesoscale on the ocean surface layer is also relatively unexplored. Using submesoscale-resolving numerical simulations, Renault et al. (2018) found a sink of energy at the submesoscale related to induced Ekman pumping velocities, but also an increase of the injection of energy by baroclinic conversion into the submesoscale. The effect of waves and Langmuir turbulence on the submesoscale processes described above is also a relatively new topic. Some studies have shown that Langmuir turbulence can significantly increase small-scale turbulence and counter the restratifying effects

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of MLI (Hamlington et al., 2014), and that surface waves also have an impact on frontogenesis (Suzuki et al., 2016; Sullivan and McWilliams, 2019). A next step in our understanding of the oceanic submesoscale processes and their impact on the stratification of the ocean surface layer may require a fully interactive atmosphere as well as the wave feedbacks, which will modulate the turbulent exchanges of momentum, heat and tracers between the atmosphere and ocean.

Submesoscale currents impact the large-scale ocean circulation in many counter-intuitive ways, including upscale energy transfer to mesoscale eddies or upgradient fluxes of tracers (Klein et al., 2019). Recent studies are highlighting the global impacts of submesoscales, for example the contribution of near-surface submesoscale currents in driving vertical heat fluxes (Su et al., 2018, 2020) and restratifying the upper ocean (Johnson et al., 2016). The role played by submesoscale instabilities at the bottom, which has been discovered much more recently, may also be a very important ingredient for the generation of near bottom mixing, the export of buoyancy and ultimately for the closure of the overturning circulation.

The current generation of OGCM is far from being able to resolve the full range of submesoscale processes in the surface and bottom boundary layers. In the ongoing CMIP6 exercise, ocean models will typically have a 1/4 degree resolution, allowing for mesoscales but not totally resolving them (Griffies et al., 2016). One can expect that truly mesoscale-resolving ocean models will be a standard for climate studies a decade from now, but the use of submesoscale-resolving models in climate studies might still be several decades away – up to 40-50 years based on Moore's law (Dong et al., 2020b). More precisely,

according to the global estimates of Dong et al. (2020b) and Dong et al. (2021) (see Fig. 8.6), the required grid spacing to resolve MLI over 90 % of the ocean's surface is about 1 km in winter and 500 m in summer, for BMLI it falls to about 100 m, and finally less than 10 m for SI. The current state-of-the-art for global or basin-scale forced ocean simulations have grid spacings on the order of 1-2 km (LLC4320 at 1/48°, eNATL60 at 1/60°, or GIGATL1 at 1 km), which can

km (LLC4320 at 1/48°, eNATL60 at 1/60°, or GIGATL1 at 1 km), which can only be said to safely resolve winter MLI. Thus, these state-of-the-art models just scratch the surface of the submesoscale realm.

While submesoscales are not fully resolved in many models, many submesoscale effects on mixing have yet to be parameterized. Some parameterizations are already used in ocean models to incorporate the restratifying effects of MLI (Fox-Kemper et al., 2011; Calvert et al., 2020) and the extraction of energy from the geostrophic currents and diffusive tracer mixing due to SI and associated secondary shear instabilities (Bachman et al., 2017a; Dong et al., 2020c). These efforts are encouraging but these parameterizations still have issues (Calvert

et al., 2020) and do not account yet for all the effects of submesoscales in the surface boundary layer. Furthermore, no parameterizations exist yet for bottom boundary submesoscale processes, and given their potential impact on the large-scale circulation, designing one should stand out as an important objective. The nonlinear, interacting processes active at the submesoscale makes the pa-

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<sup>1375</sup> rameterization problem particularly challenging. However, recent developments in empirical data-driven methods and machine learning offer a promising path forward.

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